

Topics	What students need to learn:		
	Content	Guidance	
8 Integration	8.1	Know and use the Fundamental Theorem of Calculus	Integration as the reverse process of differentiation. Students should know that for indefinite integrals a constant of integration is required.
	8.2	<p>Integrate x^n (excluding $n = -1$) and related sums, differences and constant multiples.</p> <p>Integrate e^{kx}, $\frac{1}{x}$, $\sin kx$, $\cos kx$ and related sums, differences and constant multiples.</p>	<p>For example, the ability to integrate expressions such as $\frac{1}{2}x^2 - 3x^{-\frac{1}{2}}$ and $\frac{(x+2)^2}{x^{\frac{1}{2}}}$ is expected. x</p> <p>Given $f'(x)$ and a point on the curve, Students should be able to find an equation of the curve in the form $y = f(x)$.</p> <p>To include integration of standard functions such as $\sin 3x$, $\sec^2 2x$, $\tan x$, e^{5x}, $\frac{1}{2x}$.</p> <p>Students are expected to be able to use trigonometric identities to integrate, for example, $\sin^2 x$, $\tan^2 x$, $\cos^2 3x$.</p>

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8 Integration <i>continued</i>	8.3	Evaluate definite integrals; use a definite integral to find the area under a curve and the area between two curves	<p>Students will be expected to be able to evaluate the area of a region bounded by a curve and given straight lines, or between two curves. This includes curves defined parametrically.</p> <p>For example, find the finite area bounded by the curve $y = 6x - x^2$ and the line $y = 2x$</p> <p>Or find the finite area bounded by the curve $y = x^2 - 5x + 6$ and the curve $y = 4 - x^2$.</p>
	8.4	Understand and use integration as the limit of a sum.	Recognise $\int_a^b f(x) dx = \lim_{\delta x \rightarrow 0} \sum_{x=a}^b f(x) \delta x$
	8.5	Carry out simple cases of integration by substitution and integration by parts; understand these methods as the inverse processes of the chain and product rules respectively (Integration by substitution includes finding a suitable substitution and is limited to cases where one substitution will lead to a function which can be integrated; integration by parts includes more than one application of the method but excludes reduction formulae.)	<p>Students should recognise integrals of the form $\int \frac{f'(x)}{f(x)} dx = \ln f(x) + c$.</p> <p>The integral $\int \ln x dx$ is required</p> <p>Integration by substitution includes finding a suitable substitution and is limited to cases where one substitution will lead to a function which can be integrated; integration by parts includes more than one application of the method but excludes reduction formulae.</p>
	8.6	Integrate using partial fractions that are linear in the denominator.	<p>Integration of rational expressions such as those arising from partial fractions,</p> <p>e.g. $\frac{2}{3x+5}$</p> <p>Note that the integration of other rational expressions, such as $\frac{x}{x^2+5}$ and $\frac{2}{(2x-1)^4}$ is also required (see previous paragraph).</p>
	8.7	Evaluate the analytical solution of simple first order differential equations with separable variables, including finding particular solutions (Separation of variables may require factorisation involving a common factor.)	Students may be asked to sketch members of the family of solution curves.

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8 Integration <i>continued</i>	8.8	Interpret the solution of a differential equation in the context of solving a problem, including identifying limitations of the solution; includes links to kinematics.	The validity of the solution for large values should be considered.