

TRIGONOMETRIC EQUATIONS

4) a)

$$3 \sin^2 \theta - 2 \cos^2 \theta = 1$$

$$3 \sin^2 \theta - 2(1 - \sin^2 \theta) = 1$$

$$3 \sin^2 \theta - 2 + 2 \sin^2 \theta = 1$$

$$5 \sin^2 \theta = 1 + 2$$

$$5 \sin^2 \theta = 3$$

b)

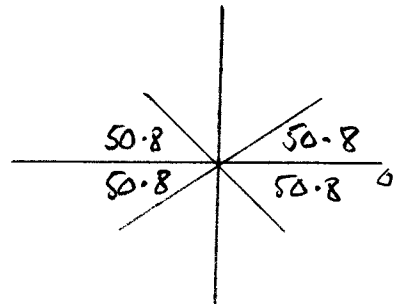
$$3 \sin^2 \theta - 2 \cos^2 \theta = 1$$

$$\Rightarrow 5 \sin^2 \theta = 3$$

$$\Rightarrow \sin^2 \theta = \frac{3}{5}$$

$$\Rightarrow \sin \theta = \pm \sqrt{\frac{3}{5}}$$

$$\sin^{-1} \sqrt{\frac{3}{5}} = 50.8^\circ$$



$$\theta = 50.8^\circ, 129.2^\circ, 230.8^\circ, 309.2^\circ$$

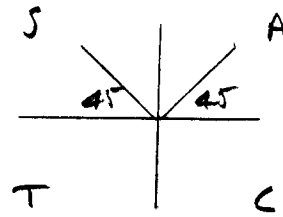
TRIGONOMETRIC EQUATIONS

9) a)

$$\sin(x - 20^\circ) = \frac{1}{\sqrt{2}}$$

$$\sin^{-1} \frac{1}{\sqrt{2}} = 45^\circ$$

$$x - 20^\circ = 45^\circ, 135^\circ$$



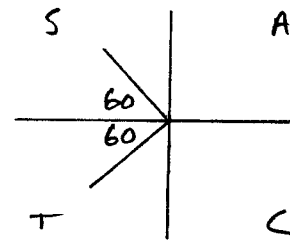
$$x = 45^\circ + 20^\circ, 135^\circ + 20^\circ$$

$$x = 65^\circ, 155^\circ$$

b)

$$\cos 3x = -\frac{1}{2}$$

$$\cos^{-1} \frac{1}{2} = 60^\circ$$



$$3x = 120^\circ, 240^\circ, 120^\circ + 360^\circ, 240^\circ + 360^\circ, 120^\circ + 720^\circ, 240^\circ + 720^\circ$$

$$3x = 120^\circ, 240^\circ, 480^\circ, 600^\circ, 840^\circ, 960^\circ$$

$$x = 40^\circ, 80^\circ, 160^\circ, 200^\circ, 280^\circ, 320^\circ$$

TRIGONOMETRIC EQUATIONS

8) a)

$$4 \sin^2 x + 9 \cos x - 6 = 0$$

$$4(1 - \cos^2 x) + 9 \cos x - 6 = 0$$

$$4 - 4 \cos^2 x + 9 \cos x - 6 = 0$$

$$0 = 4 \cos^2 x - 9 \cos x + 6 - 4$$

$$0 = 4 \cos^2 x - 9 \cos x + 2$$

b)

Solve for $0 \leq x \leq 720^\circ$

$$4 \sin^2 x + 9 \cos x - 6 = 0$$

$$\Rightarrow 4 \cos^2 x - 9 \cos x + 2 = 0$$

$$(4 \cos x - 1)(\cos x - 2) = 0$$

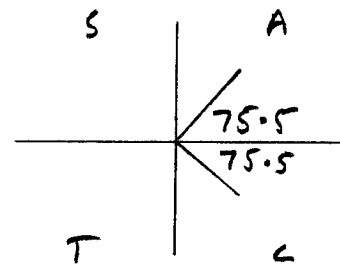
$$\Rightarrow 4 \cos x - 1 = 0$$

since $\cos x \neq 2$

$$4 \cos x = 1$$

$$\cos x = \frac{1}{4}$$

$$\cos^{-1} \frac{1}{4} = 75.5^\circ$$



$$x = 75.5^\circ, 284.5^\circ, 75.5^\circ + 360^\circ, 284.5^\circ + 360^\circ$$

$$x = 75.5^\circ, 284.5^\circ, 435.5^\circ, 644.5^\circ$$

TRIGONOMETRIC EQUATIONS

7) i)

Solve for $-180^\circ \leq \theta < 180^\circ$

$$(1 + \tan \theta)(5 \sin \theta - 2) = 0$$

$$\Rightarrow 1 + \tan \theta = 0$$

$$\text{or } 5 \sin \theta - 2 = 0$$

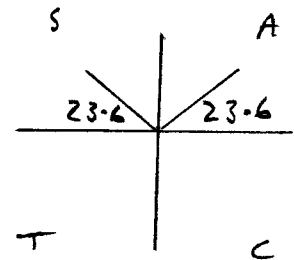
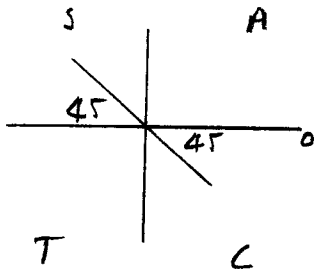
$$\tan \theta = -1$$

$$5 \sin \theta = 2$$

$$\sin \theta = \frac{2}{5}$$

$$\tan^{-1} 1 = 45^\circ$$

$$\sin^{-1} \frac{2}{5} = 23.6^\circ$$



$$\theta = -45^\circ, 135^\circ$$

$$\theta = 23.6^\circ, 156.4^\circ$$

ii)

Solve for $0^\circ \leq x < 360^\circ$

$$4 \sin x = 3 \tan x$$

$$4 \sin x = 3 \frac{\sin x}{\cos x}$$

$$4 \sin x \cos x = 3 \sin x$$

$$4 \sin x \cos x - 3 \sin x = 0$$

$$\sin x (4 \cos x - 3) = 0$$

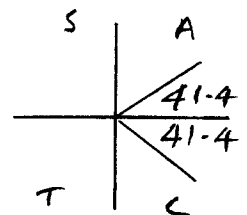
$$\Rightarrow \sin x = 0 \text{ or } 4 \cos x - 3 = 0$$

$$4 \cos x = 3$$

$$\cos x = \frac{3}{4}$$

$$x = 0^\circ, 180^\circ, 360^\circ$$

$$\cos^{-1} \frac{3}{4} = 41.4^\circ$$



$$x = 41.4^\circ, 318.6^\circ$$

$$x = 0^\circ, 180^\circ, 41.4^\circ, 318.6^\circ$$

TRIGONOMETRIC EQUATIONS

2) a)

$$5 \sin x = 1 + 2 \cos^2 x$$

$$5 \sin x = 1 + 2(1 - \sin^2 x)$$

$$5 \sin x = 1 + 2 - 2 \sin^2 x$$

$$2 \sin^2 x + 5 \sin x - 3 = 0$$

b)

$$2 \sin^2 x + 5 \sin x - 3 = 0$$

Solve for $0 \leq x < 360^\circ$

$$(2 \sin x - 1)(\sin x + 3) = 0$$

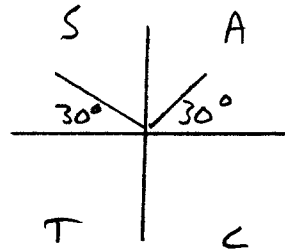
$$\Rightarrow 2 \sin x - 1 = 0$$

since $\sin x \neq -3$

$$2 \sin x = 1$$

$$\sin x = \frac{1}{2}$$

$$\sin^{-1} \frac{1}{2} = 30^\circ$$



$$x = 30^\circ, 150^\circ$$

TRIGONOMETRIC EQUATIONS

5) a)

$$5 \sin \theta = 2 \cos \theta$$

$$\frac{\sin \theta}{\cos \theta} = \frac{2}{5}$$

$$\tan \theta = \frac{2}{5}$$

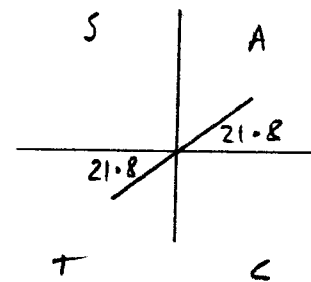
b)

$$5 \sin 2x = 2 \cos 2x$$

$$\Rightarrow \tan 2x = \frac{2}{5}$$

Solve for $0 \leq x < 360^\circ$

$$\tan^{-1} \frac{2}{5} = 21.8^\circ$$



$$2x = 21.8^\circ, 201.8^\circ, 21.8^\circ + 360^\circ, 201.8^\circ + 360^\circ$$

$$2x = 21.8^\circ, 201.8^\circ, 381.8^\circ, 561.8^\circ$$

$$x = 10.9^\circ, 100.9^\circ, 190.9^\circ, 280.9^\circ$$