

# Mark Scheme (Results) Summer 2010

GCE

## Core Mathematics C1 (6663)

Question Number	Scheme	Marks
2.	$\frac{8x^4}{4} + \frac{6x^{\frac{3}{2}}}{\frac{3}{2}} - 5x + c$ $= 2x^4 + 4x^{\frac{3}{2}} - 5x + c$	<p>M1 A1</p> <p>A1 A1</p> <p style="text-align: right;"><b>4</b></p>
<b>Notes</b>		
<p>M1 for some attempt to integrate a term in <math>x</math>: <math>x^n \rightarrow x^{n+1}</math></p> <p>1<sup>st</sup> A1 for correct, possibly un-simplified <math>x^4</math> or <math>x^{\frac{3}{2}}</math> term. e.g. <math>\frac{8x^4}{4}</math> or <math>\frac{6x^{\frac{3}{2}}}{\frac{3}{2}}</math></p> <p>2<sup>nd</sup> A1 for <u>both</u> <math>2x^4</math> and <math>4x^{\frac{3}{2}}</math> terms correct and simplified on the same line  N.B. some candidates write <math>4\sqrt{x^3}</math> or <math>4x^{1\frac{1}{2}}</math> which are, of course, fine for A1</p> <p>3<sup>rd</sup> A1 for <math>-5x + c</math>. Accept <math>-5x^1 + c</math>.  The <math>+c</math> must appear on the same line as the <math>-5x</math>  N.B. We do not need to see one line with a fully correct integral</p> <p>Ignore ISW (ignore incorrect subsequent working) if a correct answer is followed by an incorrect version.</p> <p>Condone poor use of notation e.g. <math>\int 2x^4 + 4x^{\frac{3}{2}} - 5x + c</math> will score full marks.</p>		

Question Number	Scheme	Marks
7.	$\frac{3x^2 + 2}{x} = 3x + 2x^{-1}$ $(y' =) 24x^2, -2x^{-\frac{1}{2}}, +3 - 2x^{-2}$ $\left[ 24x^2 - 2x^{-\frac{1}{2}} + 3 - 2x^{-2} \right]$	M1 A1 M1 A1 A1A1
<b>Notes</b>		
<p>1<sup>st</sup> M1 for attempting to divide (one term correct)</p> <p>1<sup>st</sup> A1 for both terms correct on the same line, accept <math>3x^1</math> for <math>3x</math> or <math>\frac{2}{x}</math> for <math>2x^{-1}</math></p> <p>These first two marks may be implied by a correct differentiation at the end.</p> <p>2<sup>nd</sup> M1 for an attempt to differentiate <math>x^n \rightarrow x^{n-1}</math> for at least one term of their expression</p> <p>“Differentiating” <math>\frac{3x^2 + 2}{x}</math> and getting <math>\frac{6x}{1}</math> is M0</p> <p>2<sup>nd</sup> A1 for <math>24x^2</math> only</p> <p>3<sup>rd</sup> A1 for <math>-2x^{-\frac{1}{2}}</math> allow <math>\frac{-2}{\sqrt{x}}</math>. Must be simplified to this, not e.g. <math>\frac{-4}{2}x^{-\frac{1}{2}}</math></p> <p>4<sup>th</sup> A1 for <math>3 - 2x^{-2}</math> allow <math>\frac{-2}{x^2}</math>. Both terms needed. Condone <math>3 + (-2)x^{-2}</math></p> <p>If “+c” is included then they lose this final mark</p> <p>They do not need one line with all terms correct for full marks. Award marks when first seen in this question and apply ISW.</p> <p>Condone a mixed line of some differentiation and some division e.g. <math>24x^2 - 4x^{\frac{1}{2}} + 3x + 2x^{-1}</math> can score 1<sup>st</sup> M1A1 and 2<sup>nd</sup> M1A1</p>		
Quotient /Product Rule	$\frac{x(6x) - (3x^2 + 2) \times 1}{x^2}$ or $6x(x^{-1}) + (3x^2 + 2)(-x^{-2})$ $\frac{3x^2 - 2}{x^2}$ or $3 - \frac{2}{x^2}$ (o.e.)	1 <sup>st</sup> M1 for an attempt: $\frac{P-Q}{x^2}$ or $R + (-S)$ with one of $P, Q$ or $R, S$ correct. 1 <sup>st</sup> A1 for a correct expression 4 <sup>th</sup> A1 same rules as above

Question Number	Scheme	Marks
11.	<p>(a) <math>(y =) \frac{3x^2}{2} - \frac{5x^{\frac{1}{2}}}{\frac{1}{2}} - 2x (+c)</math></p> <p><math>f(4) = 5 \Rightarrow 5 = \frac{3}{2} \times 16 - 10 \times 2 - 8 + c</math></p> <p style="text-align: right;"><u><math>c = 9</math></u></p> <p><math>\left[ f(x) = \frac{3}{2}x^2 - 10x^{\frac{1}{2}} - 2x + 9 \right]</math></p> <p>(b) <math>m = 3 \times 4 - \frac{5}{2} - 2 \left( = 7.5 \text{ or } \frac{15}{2} \right)</math></p> <p>Equation is: <math>y - 5 = \frac{15}{2}(x - 4)</math></p> <p style="text-align: center;"><u><math>2y - 15x + 50 = 0</math></u> o.e.</p>	<p>M1A1A1</p> <p>M1</p> <p>A1 (5)</p> <p>M1</p> <p>M1A1</p> <p>A1 (4)</p> <p>(9marks)</p>
Normal	<p>(a) 1<sup>st</sup> M1 for an attempt to integrate <math>x^n \rightarrow x^{n+1}</math></p> <p>1<sup>st</sup> A1 for at least 2 correct terms in <math>x</math> (unsimplified)</p> <p>2<sup>nd</sup> A1 for all 3 terms in <math>x</math> correct (condone missing <math>+c</math> at this point). Needn't be simplified</p> <p>2<sup>nd</sup> M1 for using the point (4, 5) to form a linear equation for <math>c</math>. Must use <math>x = 4</math> and <math>y = 5</math> and have no <math>x</math> term and the function must have "changed".</p> <p>3<sup>rd</sup> A1 for <math>c = 9</math>. The final expression is not required.</p> <p>(b) 1<sup>st</sup> M1 for an attempt to evaluate <math>f'(4)</math>. Some correct use of <math>x = 4</math> in <math>f'(x)</math> but condone slips. They must therefore have at least <math>3 \times 4</math> or <math>-\frac{5}{2}</math> and clearly be using <math>f'(x)</math> with <math>x = 4</math>. Award this mark wherever it is seen.</p> <p>2<sup>nd</sup> M1 for using their value of <math>m</math> [or their <math>-\frac{1}{m}</math>] (provided it clearly comes from using <math>x = 4</math> in <math>f'(x)</math>) to form an equation of the line through (4,5).</p> <p>Allow this mark for an attempt at a normal or tangent. Their <math>m</math> must be numerical. Use of <math>y = mx + c</math> scores this mark when <math>c</math> is found.</p> <p>1<sup>st</sup> A1 for any correct expression for the equation of the line</p> <p>2<sup>nd</sup> A1 for any correct equation with integer coefficients. An "=" is required. e.g. <math>2y = 15x - 50</math> etc as long as the equation is correct and has integer coefficients.</p> <p>Attempt at normal can score both M marks in (b) but A0A0</p>	

# Mark Scheme (Results) Summer 2010

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## Core Mathematics C2 (6664)

Question Number	Scheme	Marks
3	(a) $\left(\frac{dy}{dx} =\right) 2x - \frac{1}{2}kx^{\frac{1}{2}}$ (Having an extra term, e.g. +C, is A0)	M1 A1  (2)
	(b) Substituting $x = 4$ into their $\frac{dy}{dx}$ and ‘compare with zero’ (The mark is allowed for : $<, >, =, \leq, \geq$ )  $8 - \frac{k}{4} < 0 \quad k > 32 \quad (\text{or } 32 < k) \quad \underline{\text{Correct inequality needed}}$	M1  A1  (2) 4
	(a) M: $x^2 \rightarrow cx$ or $k\sqrt{x} \rightarrow cx^{\frac{1}{2}}$ ( $c$ constant, $c \neq 0$ )  (b) Substitution of $x = 4$ into $y$ scores M0. However, $\frac{dy}{dx}$ is sometimes <u>called</u> $y$ , and in this case the M mark can be given.  $\frac{dy}{dx} = 0$ may be ‘implied’ for M1, when, for example, a value of $k$ or an inequality solution for $k$ is found.  <u>Working</u> must be seen to justify marks in (b), i.e. $k > 32$ alone is M0 A0.	

Question Number	Scheme	Marks
8	<p>(a) <math>\frac{dy}{dx} = 3x^2 - 20x + k</math> (Differentiation is required)</p> <p>At <math>x = 2</math>, <math>\frac{dy}{dx} = 0</math>, so <math>12 - 40 + k = 0</math> <math>k = 28</math> (*)</p> <p><u>N.B. The ' = 0 ' must be seen at some stage to score the final mark.</u></p> <p>Alternatively: (using <math>k = 28</math>)</p> <p><math>\frac{dy}{dx} = 3x^2 - 20x + 28</math> (M1 A1)</p> <p>'Assuming' <math>k = 28</math> only scores the final cso mark if there is justification that <math>\frac{dy}{dx} = 0</math> at <math>x = 2</math> represents the <u>maximum</u> turning point.</p>	M1 A1 A1 cso (3)
	<p>(b) <math>\int (x^3 - 10x^2 + 28x) dx = \frac{x^4}{4} - \frac{10x^3}{3} + \frac{28x^2}{2}</math> Allow <math>\frac{kx^2}{2}</math> for <math>\frac{28x^2}{2}</math></p> <p><math>\left[ \frac{x^4}{4} - \frac{10x^3}{3} + 14x^2 \right]_0^2 = \dots</math> <math>\left( = 4 - \frac{80}{3} + 56 = \frac{100}{3} \right)</math></p> <p>(With limits 0 to 2, substitute the limit 2 into a 'changed function')</p> <p>y-coordinate of <math>P = 8 - 40 + 56 = 24</math> Allow if seen in part (a) (The B1 for 24 may be scored by implication from later working)</p> <p>Area of rectangle = <math>2 \times</math> (their y - coordinate of <math>P</math>)</p> <p>Area of <math>R =</math> (their 48) <math>-</math> <math>\left( \text{their } \frac{100}{3} \right) = \frac{44}{3} \left( 14\frac{2}{3} \text{ or } 14.\dot{6} \right)</math></p> <p>If the subtraction is the 'wrong way round', the final A mark is lost.</p>	M1 A1 M1 B1 M1 A1 (6) 9
	<p>(a) M: <math>x^n \rightarrow cx^{n-1}</math> (<math>c</math> constant, <math>c \neq 0</math>) for one term, seen in part (a).</p> <p>(b) 1<sup>st</sup> M: <math>x^n \rightarrow cx^{n+1}</math> (<math>c</math> constant, <math>c \neq 0</math>) for one term. Integrating the <u>gradient function</u> loses this M mark.</p> <p>2<sup>nd</sup>M: Requires use of limits 0 and 2, with 2 substituted into a 'changed function'. (It may, for example, have been differentiated).</p> <p>Final M: Subtract their values either way round. This mark is dependent on the use of calculus and a correct method attempt for the area of the rectangle.</p> <p>A1: Must be <u>exact</u>, not 14.67 or similar, but isw after seeing, say, <math>\frac{44}{3}</math>.</p> <p><u>Alternative:</u> (effectively finding area of rectangle by integration)</p> <p><math>\int \{24 - (x^3 - 10x^2 + 28x)\} dx = 24x - \left( \frac{x^4}{4} - \frac{10x^3}{3} + \frac{28x^2}{2} \right)</math>, etc.</p> <p>This can be marked equivalently, with the 1<sup>st</sup> A being for integrating the same 3 terms correctly. The 3<sup>rd</sup> M (for subtraction) will be scored at the same stage as the 2<sup>nd</sup> M. If the subtraction is the 'wrong way round', the final A mark is lost.</p>	