

Linear Equations 2

Recap

$$1) \quad 3x + 7 = 23$$

$$3x = 23 - 7$$

$$3x = 16$$

$$x = \frac{16}{3}$$

$$x = 5\frac{1}{3}$$

$$2) \quad 4x + 37 = 19$$

$$4x = 19 - 37$$

$$4x = -18$$

$$x = -\frac{18}{4}$$

$$x = -\frac{9}{2}$$

$$x = -4\frac{1}{2}$$

Exercise

$$1) \quad 5x + 27 = 42$$

$$5x = 42 - 27$$

$$5x = 15$$

$$x = \frac{15}{5}$$

$$\underline{x = 3}$$

$$2) \quad 7x - 3 = 17$$

$$7x = 17 + 3$$

$$7x = 20$$

$$x = \frac{20}{7}$$

$$\underline{x = 2\frac{6}{7}}$$

Eqns with x on both sides

Ex 1

$$8x - 11 = 5x + 19$$

$$8x - 5x = +19 + 11$$

$$3x = 30$$

$$x = \frac{30}{3}$$

$$\underline{x = 10}$$

Ex2

$$7x + 8 = 20 - 3x$$

$$7x + 3x = 20 - 8$$

$$10x = 12$$

$$x = \frac{12}{10}$$

$$x = \frac{6}{5}$$

$$x = 1\frac{1}{5}$$

Exercise

$$1) \quad 9x - 8 = 5x + 32 \quad 2) \quad 4x + 13 = 53 - x$$

$$9x - 5x = 32 + 8$$

$$4x = 40$$

$$x = \frac{40}{4}$$

$$\underline{x = 10}$$

$$4x + x = 53 - 13$$

$$5x = 40$$

$$x = \frac{40}{5}$$

$$\underline{x = 8}$$

Equations involving brackets

Ex1

$$3(2x + 5) = 33$$

$$6x + 15 = 33$$

$$6x = 33 - 15$$

$$6x = 18$$

$$x = \frac{18}{6}$$

$$\underline{x = 3}$$

$$3(2x + 5) = 33$$

$$2x + 5 = \frac{33}{3}$$

$$2x + 5 = 11$$

$$2x = 11 - 5$$

$$2x = 6$$

$$\underline{x = 3}$$

Ex2

$$4(x+1) = 3(3x+5) - 7$$

$$4x + 4 = 9x + 15 - 7$$

$$4x - 9x = +15 - 7 - 4$$

$$-5x = 4$$

$$x = \frac{4}{-5}$$

$$\underline{x = -\frac{4}{5}}$$

Exercise

$$1) 5(2x - 3) = 25$$

$$10x - 15 = 25$$

$$10x = 25 + 15$$

$$10x = 40$$

$$x = \frac{40}{10}$$

$$\underline{x = 4}$$

$$2) 7(x+2) = 8(2x-1) - 5$$

$$7x + 14 = 16x - 8 - 5$$

$$7x - 16x = -8 - 5 - 14$$

$$-9x = -27$$

$$x = \frac{-27}{-9}$$

$$\underline{x = 3}$$

Problem Solving

Ex1 Bill is twice as old as Alan. Colin is 5 years older than Bill. Colin is 17.
How old is Alan?

Let Alan be x

Bill = $2x$

Colin = $2x + 5$

$$2x + 5 = 17$$

$$2x = 17 - 5$$

$$2x = 12$$

$$x = \frac{12}{2}$$

$$\underline{x = 6}$$

Ex 2

John's dad is three times as old as John
In 12 years time his dad will be only
twice as old as John. How old is John
now?

Let John be x years old now
Dad now = $3x$

In 12 years time John = $x + 12$

Dad = $3x + 12$

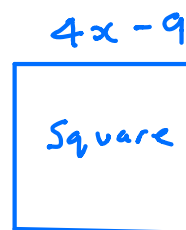
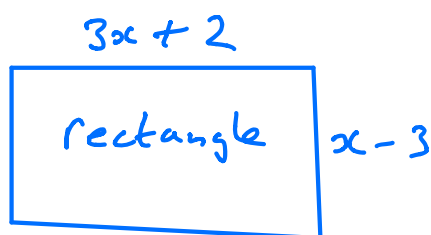
$$3x + 12 = 2(x + 12)$$

$$3x + 12 = 2x + 24$$

$$3x - 2x = 24 - 12$$

$$\underline{x = 12}$$

Ex 3



Rectangle and square have same perimeter
What is this perimeter

$$\begin{aligned}\text{Perimeter of Square} &= 4(4x-9) \\ &= 16x-36\end{aligned}$$

$$\text{Perimeter of Rectangle}$$

$$= 3x+2 + x-3 + 3x+2 + x-3 = 8x-2$$

$$16x-36 = 8x-2$$

$$16x-8x = -2+36$$

$$8x = 34$$

$$x = \frac{34}{8}$$

$$x = \frac{17}{4}$$

$$\underline{x = 4.25}$$

$$\begin{aligned}\text{Perimeter of each shape} &= 8 \times 4.25 - 2 \\ &= 32 \quad \checkmark\end{aligned}$$

$$\text{or } 16 \times 4.25 - 36 = 32 \quad \checkmark$$
