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14 Solve, algebraically, these simultaneous equations.

$$\begin{array}{l} 2x - 3y = 14 \\ 6x + 4y = 3 \end{array}$$

(1)
(2)

$$(1) \times 4 \quad 8x - 12y = 56 \quad (3)$$

$$(2) \times 3 \quad 18x + 12y = 9 \quad (4)$$

$$\begin{array}{rcl} (3) + (4) & 26x & = 65 \\ & x & = \frac{65}{26} \end{array}$$

$$\underline{x = 2\frac{1}{2}}$$

Solution

Sub for x in (2)

$$x = 2\frac{1}{2}$$

$$\begin{array}{rcl} 15 + 4y & = 3 \\ 4y & = 3 - 15 \\ 4y & = -12 \\ y & = -\frac{12}{4} \\ y & = -3 \end{array}$$

$$y = -3$$

16 (a) Solve, algebraically, these simultaneous equations.

$$\begin{array}{l} 3x - 5y = 111 \\ 4x + 3y = -26 \end{array}$$

(1)
(2)

$$(1) \times 3 \quad 9x - 15x = 333 \quad (3)$$

$$(2) \times 5 \quad 20x + 15x = -130 \quad (4)$$

$$(3) + (4) \quad 29x = 203$$

$$x = \frac{203}{29} = 7$$

Sub for x in ②

$$4(7) + 3y = -26$$

$$28 + 3y = -26$$

$$3y = -26 - 28$$

$$3y = -54$$

$$y = -\frac{54}{3}$$

$$y = -18$$

$$\begin{cases} x = 7 \\ y = -18 \end{cases}$$

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14 Solve these simultaneous equations algebraically.

$$\begin{aligned} 3x + y &= 13 \\ 2x - y &= 12 \end{aligned}$$

①
②

① + ②

$$5x = 25$$

$$x = \frac{25}{5} = 5$$

Sub for x in ①

$$3(5) + y = 13$$

$$15 + y = 13$$

$$y = 13 - 15$$

$$y = -2$$

$$\begin{cases} x = 5 \\ y = -2 \end{cases}$$

12 Solve algebraically these simultaneous equations.

$$3x - y = 1$$

$$5x + 3y = 4$$

①
②

① $\times 3$

$$9x - 3y = 3$$

③

② + ③

$$14x = 7$$

$$x = \frac{7}{14} = \frac{1}{2}$$

Sub for x in ②

$$\begin{aligned} \frac{5}{2} + 3y &= 4 \\ 3y &= 4 - \frac{5}{2} \\ y &= \frac{3}{2} \\ y &= \underline{\frac{3}{2}} \end{aligned}$$

2 Adults and 3 children = £28.20

3 Adults and 5 children = £44.75

Let adult ticket cost A

Let child ticket cost C

$$2A + 3C = \text{£}28.20 \quad \textcircled{1}$$

$$3A + 5C = \text{£}44.75 \quad \textcircled{2}$$

$$\textcircled{1} \times 5 \quad 10A + 15C = \text{£}141 \quad \textcircled{3}$$

$$\textcircled{2} \times 3 \quad 9A + 15C = \text{£}134.25 \quad \textcircled{4}$$

$$\textcircled{3} - \textcircled{4} \quad A = \text{£}6.75$$

$$\text{Sub in } \textcircled{1} \quad 2(6.75) + 3C = \text{£}28.20$$

$$13.50 + 3C = \text{£}28.20$$

$$3C = \text{£}28.20 - \text{£}13.50$$

$$\text{Adult } \text{£}6.75$$

$$3C = \text{£}14.70$$

$$\text{Child } \text{£}4.90$$

$$C = \underline{\frac{\text{£}14.70}{3}}$$

$$C = \text{£}4.90$$