

Exercise 2C

$$7) X \sim P_0(1.8)$$

$$a) P(X=0) = 0.1652$$

$$P(X=3) = 0.1606$$

$$P(X \geq 3) = 1 - P(X \leq 2)$$

$$= 1 - 0.7306 = 0.2694$$

$$b) Y \sim B(4, 0.2694)$$

$$P(Y=1) = 4C_1 \times 0.2694^1 \times 0.7306^3$$

$$= 0.4202$$

$$a) X \sim P_0\left(\frac{3}{4}\right) \quad \text{breakdowns per week}$$

$$a) i) P(X \geq 1) = 1 - P(X=0)$$

$$= 1 - e^{-3/4}$$

$$= 0.5276$$

$$ii) P(X=2) = \frac{e^{-3/4} \times (3/4)^2}{2!} = 0.1329$$

$$b) \text{Prob breaks down next week} = P(X \geq 1)$$

$$= 0.5276$$

Since breakdowns independent

Adding Poisson Distributions.

For independent Poisson variables X and Y

$$\text{if } X \sim P_0(\lambda) \quad \text{and} \quad Y \sim P_0(\mu)$$

$$\text{then } X+Y \sim P_0(\lambda+\mu)$$

Exercise 2D

$$7) \quad C \sim P_0(0.1 \times 12) \quad D \sim P_0(0.05 \times 12)$$

$$C \sim P(1.2) \quad D \sim P_0(0.6)$$

$$\begin{aligned} a) \quad P(C \geq 1) &= 1 - P(C=0) \\ &= 1 - e^{-1.2} = 0.6988 \end{aligned}$$

$$b) \quad P(C \geq 1 \wedge D \geq 1)$$

$$P(D \geq 1) = 1 - e^{-0.6} = 0.4512$$

$$\begin{aligned} P(C \geq 1 \wedge D \geq 1) &= 0.6988 \times 0.4512 \\ &= 0.31529856 \\ &= 0.315 \end{aligned}$$

$$c) \quad Y \sim P_0(1.2 + 0.6) = P_0(1.8)$$

$$P(Y=3) = 0.1607$$

Classwork and Homework

Exercise 2C Q 8, 10, 12, 14

Exercise 2D Q 6, 8, 10
