| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $X \sim$ females $X \sim \mathrm{~N}\left(165,9^{2}\right), Y \sim$ males $Y \sim \mathrm{~N}\left(178,10^{2}\right)$ | M1 | 3.3 | 5th <br> Calculate probabilities for the standard normal distribution using a calculator. |
|  | $\mathrm{P}(X>177)=\mathrm{P}(Z>1.33)($ or $=0.0912)$ | M1 | 1.1b |  |
|  | $\mathrm{P}(Y>190)=\mathrm{P}(Z>1.20)($ or $=0.1151)$ | A1 | 1.1b |  |
|  | Therefore the females are relatively taller. | A1 | 2.2a |  |
| (4 marks) |  |  |  |  |
| Notes |  |  |  |  |


| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 2a | $\mathrm{P}(M<850)=0.3085$ (using calculator) | B1 | 1.1b | 5th |
|  |  |  |  | Calculate probabilities for the standard normal distribution using a calculator. |
|  |  | (1) |  |  |
| 2b | $\mathrm{P}(M<a)=0.1$ and $\mathrm{P}(M<b)=0.9$ | M1 | 3.1b | 5th <br> Calculate probabilities for the standard normal distribution using a calculator. |
|  | (using calculator) $a=772 \mathrm{~g}$ | A1 | 1.1b |  |
|  | $b=1028 \mathrm{~g}$ | A1 | 1.1b |  |
|  |  | (3) |  |  |
|  |  |  |  | (4 marks) |
| Notes |  |  |  |  |


| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 3 | $X \sim \mathrm{~B}(200,0.54)$ | B1 | 3.3 | 7th <br> Use the normal distribution to approximate a binomial distribution. |
|  | $Y \sim \mathrm{~N}(108,49.68)$ | B2 | 3.1b |  |
|  | $\mathrm{P}(X>100)=\mathrm{P}(X \geqslant 101)$ | M1 | 3.4 |  |
|  | $=\mathrm{P}\left(Z \geqslant \frac{100.5-108}{\sqrt{49.68}}\right)$ | M1 | 1.1b |  |
|  | $=\mathrm{P}(\mathrm{Z} \geqslant-1.06 \ldots)=0.8554$ | A1 | 1.1 b |  |
|  |  |  |  | ( 6 marks) |
| Notes |  |  |  |  |


| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 4a |  | B1 | 1.2 | 5th <br> Understand the basic features of the normal distribution including parameters, shape and notation. |
|  | 170, 180 on axis | B1 | 1.1b |  |
|  | 5\% and 20\% | B1 | 1.1b |  |
|  |  | (3) |  |  |
| 4b | $\begin{aligned} & \mathrm{P}(X<170)=0.05 \\ & \frac{170-\mu}{\sigma}=-1.6449 \\ & \mu=170+1.6449 \sigma \\ & \mathrm{P}(X>180)=0.2 \\ & \mu=180-0.8416 \sigma \end{aligned}$ <br> Solving simultaneously gives: $\mu=176.615 \ldots(\text { awrt } 176.6) \text { and } \sigma=4.021 \ldots(\text { awrt 4.02 })$ | $\begin{gathered} \text { M1 } \\ \text { B1 } \\ \text { B1 } \\ \text { B1 } \\ \text { M1 } \\ \text { A1 } \\ \text { A1 } \end{gathered}$ | $\begin{gathered} 3.3 \\ 3.4 \\ 1.1 \mathrm{~b} \\ 3.4 \\ 1.1 \mathrm{~b} \\ 1.1 \mathrm{~b} \\ 1.1 \mathrm{~b} \end{gathered}$ | 7th <br> Find unknown means and/or standard deviations for normal distributions. |
|  |  | (7) |  |  |
| 4c | $\mathrm{P}($ All three are taller than 175 cm$)=0.656 \ldots{ }^{3}$ | M1 | 1.1b | 5th <br> Understand informally the link to probability distributions. |
|  | $=0.282 \ldots$ (using calculator) awrt 0.282 | A1 | 1.1b |  |
|  |  | (2) |  |  |
|  |  |  |  | (12 marks) |
| Notes |  |  |  |  |


| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 5a | $n$ is large | B1 | 1.2 | 5th <br> Understand the binomial distribution (and its notation) and its use as a model. |
|  | $p$ is close to 0.5 | B1 | 1.2 |  |
|  |  | (2) |  |  |
| 5b | Mean $=n p$ | B1 | 1.2 | 5th <br> Understand the binomial distribution (and its notation) and its use as a model. |
|  | Variance $=n p(1-p)$ | B1 | 1.2 |  |
|  |  | (2) |  |  |
| 5c | There would be no batteries left. | B1 | 2.4 | 5th <br> Select and critique a sampling technique in a given context. |
|  |  | (1) |  |  |
| 5d | $\mathrm{H}_{0}: p=0.55 \quad \mathrm{H}_{1}: p>0.55$ | B1 | 2.5 | 5th <br> Carry out 1-tail tests for the binomial distribution. |
|  |  | (1) |  |  |
| 5 e | $\begin{aligned} & X \sim \mathrm{~N}(165,74.25) \\ & \mathrm{P}(X \geqslant 183.5) \\ & =\mathrm{P}\left(Z \geqslant \frac{183.5-165}{\sqrt{74.25}}\right) \\ & =\mathrm{P}(Z \geqslant 2.146 \ldots) \\ & =1-0.9838 \\ & =0.0159 \end{aligned}$ <br> Reject $\mathrm{H}_{0}$, it is in the critical region. <br> There is evidence to support the manufacturer's claim. | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \hline \end{aligned}$ | $\begin{gathered} 3.3 \\ 3.4 \\ 1.1 \mathrm{~b} \\ \\ 1.1 \mathrm{~b} \\ \\ 1.1 \mathrm{~b} \\ 1.1 \mathrm{~b} \\ 2.2 \mathrm{~b} \end{gathered}$ | 7th <br> Interpret the results of a hypothesis test for the mean of a normal distribution. |
|  |  | (7) |  |  |
| (13 marks) |  |  |  |  |
| Notes |  |  |  |  |

## Pearson Edexcel AS and A level Mathematics

| Q | Scheme | Marks | AOs | Pearson <br> Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 6a | Bell shaped. | B1 | 2.2a | 5th <br> Understand the basic features of the normal distribution including parameters, shape and notation. |
|  |  |  |  |  |
|  |  | (1) |  |  |
| 6b | $X \sim$ Daily mean pressure $X \sim \mathrm{~N}\left(1006,4.4^{2}\right)$ | M1 | 3.3 | 5th <br> Calculate probabilities for the standard normal distribution using a calculator. |
|  |  |  |  |  |
|  | $\mathrm{P}(X<1000)=0.0863$ | A1 | 1.1b |  |
|  |  | (2) |  |  |
| 6c | A sensible reason. For example, <br> The tails of a Normal distribution are infinite. <br> Cannot rule out extreme events. | B1 | 2.4 | 5th <br> Understand the basic features of the normal distribution including parameters, shape and notation |
|  |  | (1) |  |  |


| 6d | Comparison and sensible comment on means. For example, The mean daily mean pressure for Beijing is less than Jacksonville. <br> This suggests better weather in Jacksonville. <br> Comparison and sensible comment on standard deviations. For example, <br> The standard deviation for Beijing is greater than that for Jacksonville. <br> This suggests more consistent weather in Jacksonville. Student claim could be correct. | B1 B1 B1 B1 | $\begin{aligned} & 2.2 \mathrm{~b} \\ & 2.2 \mathrm{~b} \\ & 2.2 \mathrm{~b} \\ & 2.2 \mathrm{~b} \end{aligned}$ | 8th <br> Solve real-life problems in context using probability distributions. |
| :---: | :---: | :---: | :---: | :---: |
|  |  | (4) |  |  |
| (8 marks) |  |  |  |  |
| Notes <br> 6a <br> Do not accept symmetrical with no discription of the shape. <br> 6d <br> B2 for Suggests better weather in Jacksonville but less consistent. |  |  |  |  |


| Q | Scheme | Marks | AOs | Pearson Progression Step and Progress descriptor |
| :---: | :---: | :---: | :---: | :---: |
| 7a | $X \sim$ women's body temperature $X \sim \mathrm{~N}(36.73,0.1482)$ | M1 | 3.3 | 5th <br> Calculate probabilities for the standard normal distribution using a calculator. |
|  | $\mathrm{P}(X>38.1)=0.000186$ | B1 | 1.1b |  |
|  |  | (2) |  |  |
| 7b | Sensible reason. For example, <br> Call the doctor as very unlikely the temperature would be so high. | B1 | 2.2a | 8th <br> Solve real-life problems in context using probability distributions. |
|  |  | (1) |  |  |
| (3 marks) |  |  |  |  |
| Notes |  |  |  |  |

