

$$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

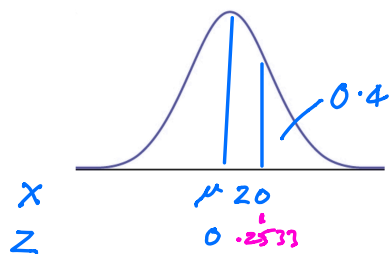
$\mu \pm \sigma$  68% of data

$\mu \pm 2\sigma$  95% of data

$\mu \pm 3\sigma$  99.75% of data

$\mu \pm 6\sigma$  1 in 500 million chance of being outside this range

Example 1



$$X \sim N(\mu, 5^2)$$

$$\text{and } P(X > 20) = 0.4$$

Find  $\mu$

$$Z = \frac{X - \mu}{\sigma}$$

$$Z = \Phi^{-1}(0.6) = 0.2533$$

$$Z\sigma = X - \mu$$

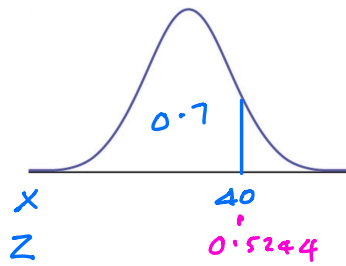
$$\mu = X - Z\sigma$$

$$\mu = 20 - 0.2533 \times 5$$

$$\mu = 18.7235$$

$$\mu = 18.7 \quad \text{to 3 s.f.}$$

## Example 2



$$X \sim N(25, \sigma^2)$$

If  $P(X < 40) = 0.7$  find  $\sigma$

$$Z = \Phi^{-1}(0.7)$$

$$Z = \frac{X - \mu}{\sigma}$$

$$\sigma Z = X - \mu$$

$$\sigma = \frac{X - \mu}{Z}$$

$$\sigma = \frac{40 - 25}{0.5244} = 28.6$$

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Hwk Read pages 37 - 47