

Topics	What students need to learn:		
	Content	Guidance	
5 Trigonometry	5.1	<p><b>Understand and use the definitions of sine, cosine and tangent for all arguments;</b></p> <p><b>the sine and cosine rules;</b></p> <p><b>the area of a triangle in the form <math>\frac{1}{2}ab \sin C</math></b></p> <p>Work with radian measure, including use for arc length and area of sector.</p>	<p><b>Use of <math>x</math> and <math>y</math> coordinates of points on the unit circle to give cosine and sine respectively,</b></p> <p><b>including the ambiguous case of the sine rule.</b></p> <p>Use of the formulae <math>s = r\theta</math> and <math>A = \frac{1}{2}r^2\theta</math> for arc lengths and areas of sectors of a circle.</p>
	5.2	<p>Understand and use the standard small angle approximations of sine, cosine and tangent</p> <p><math>\sin \theta \approx \theta,</math></p> <p><math>\cos \theta \approx 1 - \frac{\theta^2}{2}, \quad \tan \theta \approx \theta</math></p> <p>Where <math>\theta</math> is in radians.</p>	<p>Students should be able to approximate, e.g. <math>\frac{\cos 3x - 1}{x \sin 4x}</math> when <math>x</math> is small, to <math>-\frac{9}{8}</math></p>
	5.3	<p><b>Understand and use the sine, cosine and tangent functions; their graphs, symmetries and periodicity.</b></p> <p>Know and use exact values of sin and cos for <math>0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \frac{\pi}{2}, \pi</math> and multiples thereof, and exact values of tan for <math>0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \frac{\pi}{2}, \pi</math> and multiples thereof.</p>	<p><b>Knowledge of graphs of curves with equations such as <math>y = \sin x,</math> <math>y = \cos(x + 30^\circ), y = \tan 2x</math> is expected.</b></p>
	5.4	<p>Understand and use the definitions of secant, cosecant and cotangent and of arcsin, arccos and arctan; their relationships to sine, cosine and tangent; understanding of their graphs; their ranges and domains.</p>	<p>Angles measured in both degrees and radians.</p>

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<b>5</b> <b>Trigonometry</b> <i>continued</i>	5.5	<p><b>Understand and use</b></p> $\tan \theta = \frac{\sin \theta}{\cos \theta}$ <p><b>Understand and use</b></p> $\sin^2 \theta + \cos^2 \theta = 1$ $\sec^2 \theta = 1 + \tan^2 \theta$ and $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$	<p><b>These identities may be used to solve trigonometric equations</b> and angles may be in degrees or radians. <b>They may also be used to prove further identities.</b></p>
	5.6	<p>Understand and use double angle formulae; use of formulae for <math>\sin(A \pm B)</math>, <math>\cos(A \pm B)</math>, and <math>\tan(A \pm B)</math>, understand geometrical proofs of these formulae.</p> <p>Understand and use expressions for <math>a \cos \theta + b \sin \theta</math> in the equivalent forms of <math>r \cos(\theta \pm \alpha)</math> or <math>r \sin(\theta \pm \alpha)</math></p>	<p>To include application to half angles. Knowledge of the <math>\tan\left(\frac{1}{2}\theta\right)</math> formulae will <i>not</i> be required.</p> <p>Students should be able to solve equations such as <math>a \cos \theta + b \sin \theta = c</math> in a given interval.</p>
	5.7	<p><b>Solve simple trigonometric equations in a given interval, including quadratic equations in sin, cos and tan and equations involving multiples of the unknown angle.</b></p>	<p><b>Students should be able to solve equations such as</b></p> $\sin(x + 70^\circ) = 0.5 \text{ for } 0 < x < 360^\circ,$ $3 + 5 \cos 2x = 1 \text{ for } -180^\circ < x < 180^\circ$ $6 \cos^2 x + \sin x - 5 = 0, 0 \leq x < 360^\circ$ <p>These may be in degrees or radians and this will be specified in the question.</p>
	5.8	<p>Construct proofs involving trigonometric functions and identities.</p>	<p>Students need to prove identities such as <math>\cos x \cos 2x + \sin x \sin 2x \equiv \cos x</math>.</p>
	5.9	<p>Use trigonometric functions to solve problems in context, including problems involving vectors, kinematics and forces.</p>	<p>Problems could involve (for example) wave motion, the height of a point on a vertical circular wheel, or the hours of sunlight throughout the year. Angles may be measured in degrees or in radians.</p>