

Topics	What students need to learn:		
		Content	Guidance
<b>6</b> <b>Exponentials and logarithms</b>	6.1	<p><b>Know and use the function <math>a^x</math> and its graph, where <math>a</math> is positive.</b></p> <p><b>Know and use the function <math>e^x</math> and its graph.</b></p>	<p><b>Understand the difference in shape between <math>a &lt; 1</math> and <math>a &gt; 1</math></b></p> <p>To include the graph of <math>y = e^{ax+b} + c</math></p>
	6.2	<p><b>Know that the gradient of <math>e^{kx}</math> is equal to <math>ke^{kx}</math> and hence understand why the exponential model is suitable in many applications.</b></p>	<p><b>Realise that when the rate of change is proportional to the <math>y</math> value, an exponential model should be used.</b></p>
	6.3	<p><b>Know and use the definition of <math>\log_a x</math> as the inverse of <math>a^x</math>, where <math>a</math> is positive and <math>x \geq 0</math>.</b></p> <p><b>Know and use the function <math>\ln x</math> and its graph.</b></p> <p><b>Know and use <math>\ln x</math> as the inverse function of <math>e^x</math></b></p>	<p><math>a \neq 1</math></p> <p><b>Solution of equations of the form <math>e^{ax+b} = p</math> and <math>\ln(ax+b) = q</math> is expected.</b></p>
	6.4	<p><b>Understand and use the laws of logarithms:</b></p> <p><math>\log_a x + \log_a y = \log_a (xy)</math></p> <p><math>\log_a x - \log_a y = \log_a \left( \frac{x}{y} \right)</math></p> <p><math>k \leq \log_a x = \log_a x^k</math></p> <p><b>(including, for example, <math>k = -1</math> and <math>k = -\frac{1}{2}</math>)</b></p>	<p><b>Includes <math>\log_a a = 1</math></b></p>
	6.5	<p><b>Solve equations of the form <math>a^x = b</math></b></p>	<p><b>Students may use the change of base formula. Questions may be of the form, e.g. <math>2^{3x-1} = 3</math></b></p>
	6.6	<p><b>Use logarithmic graphs to estimate parameters in relationships of the form <math>y = ax^n</math> and <math>y = kb^x</math>, given data for <math>x</math> and <math>y</math></b></p>	<p><b>Plot <math>\log y</math> against <math>\log x</math> and obtain a straight line where the intercept is <math>\log a</math> and the gradient is <math>n</math></b></p> <p><b>Plot <math>\log y</math> against <math>x</math> and obtain a straight line where the intercept is <math>\log k</math> and the gradient is <math>\log b</math></b></p>

Topics	What students need to learn:		
		Content	Guidance
<b>6</b> <b>Exponentials and logarithms</b> <i>continued</i>	6.7	<b>Understand and use exponential growth and decay; use in modelling (examples may include the use of e in continuous compound interest, radioactive decay, drug concentration decay, exponential growth as a model for population growth); consideration of limitations and refinements of exponential models.</b>	<b>Students may be asked to find the constants used in a model.</b>  <b>They need to be familiar with terms such as initial, meaning when <math>t = 0</math>.</b>  <b>They may need to explore the behaviour for large values of <math>t</math> or to consider whether the range of values predicted is appropriate.</b>  <b>Consideration of a second improved model may be required.</b>