| Topics | What students need to learn: |  |  |
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|  | Content |  | Guidance |
| 2 <br> Algebra and functions | 2.1 | Understand and use the laws of indices for all rational exponents. | $a^{m} \times a^{n}=a^{m+n}, a^{m} \div a^{n}=a^{m-n},\left(a^{m}\right)^{n}=a^{m n}$ <br> The equivalence of $a^{\frac{m}{n}}$ and $\sqrt[n]{a^{m}}$ should be known. |
|  | 2.2 | Use and manipulate surds, including rationalising the denominator. | Students should be able to simplify algebraic surds using the results $\begin{aligned} & (\sqrt{x})^{2}=x, \sqrt{x y}=\sqrt{x} \sqrt{y} \text { and } \\ & (\sqrt{x}+\sqrt{y})(\sqrt{x}-\sqrt{y})=x-y \end{aligned}$ |
|  | 2.3 | Work with quadratic functions and their graphs. <br> The discriminant of a quadratic function, including the conditions for real and repeated roots. <br> Completing the square. <br> Solution of quadratic equations <br> including solving quadratic equations in a function of the unknown. | The notation $\mathrm{f}(x)$ may be used <br> Need to know and to use $\begin{aligned} & b^{2}-4 a c>0, b^{2}-4 a c=0 \text { and } \\ & b^{2}-4 a c<0 \end{aligned}$ $a x^{2}+b x+c=a\left(x+\frac{b}{2 a}\right)^{2}+\left(c-\frac{b^{2}}{4 a}\right)$ <br> Solution of quadratic equations by factorisation, use of the formula, use of a calculator and completing the square. <br> These functions could include powers of $x$, trigonometric functions of $x$, exponential and logarithmic functions of $x$. |
|  | 2.4 | Solve simultaneous equations in two variables by elimination and by substitution, including one linear and one quadratic equation. | The quadratic may involve powers of 2 in one unknown or in both unknowns, e.g. solve $y=2 x+3, y=x^{2}-4 x+8$ or $2 x-3 y=6, x^{2}-y^{2}+3 x=50$ |


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| 2 <br> Algebra and functions continued | 2.5 | Solve linear and quadratic inequalities in a single variable and interpret such inequalities graphically, <br> including inequalities with brackets and fractions. <br> Express solutions through correct use of 'and' and 'or', or through set notation. <br> Represent linear and quadratic inequalities such as $y>x+1$ and $y>a x^{2}+b x+c$ graphically. | e.g. solving $\begin{aligned} & a x+b>c x+d \\ & p x^{2}+q x+r \geq 0 \\ & p x^{2}+q x+r<a x+b \end{aligned}$ <br> and interpreting the third inequality as the range of $x$ for which the curve $y=p x^{2}+q x+r$ is below the line with equation $y=a x+b$ <br> These would be reducible to linear or quadratic inequalities <br> e.g. $\frac{a}{\boldsymbol{x}}<\boldsymbol{b}$ becomes $\boldsymbol{a} \boldsymbol{x}<\boldsymbol{b} \boldsymbol{x}^{2}$ <br> So, e.g. $x<a$ or $x>b$ is equivalent to $\{x: x<a\} \cup\{x: x>b\}$ <br> and $\{x: c<x\} \cap\{x: x<d\}$ is equivalent to $x>c$ and $x<d$ <br> Shading and use of dotted and solid line convention is required. |
|  | 2.6 | Manipulate polynomials algebraically, including expanding brackets and collecting like terms, factorisation and simple algebraic division; use of the factor theorem. <br> Simplify rational expressions, including by factorising and cancelling, and algebraic division (by linear expressions only). | Only division by $(a x+b)$ or $(a x-b)$ will be required. Students should know that if $\mathrm{f}(x)=0$ when $x=a$, then $(x-a)$ is a factor of $f(x)$. <br> Students may be required to factorise cubic expressions such as $x^{3}+3 x^{2}-4 \text { and } 6 x^{3}+11 x^{2}-x-6$ <br> Denominators of rational expressions will be linear or quadratic, $\text { e.g. } \frac{1}{a x+b}, \frac{a x+b}{p x^{2}+q x+r}, \frac{x^{3}+a^{3}}{x^{2}-a^{2}}$ |


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| 2 <br> Algebra and functions <br> continued | 2.7 | Understand and use graphs of functions; sketch curves defined by simple equations including polynomials <br> The modulus of a linear function. $y=\frac{a}{x} \quad \text { and } \quad y=\frac{a}{x^{2}}$ <br> (including their vertical and horizontal asymptotes) <br> Interpret algebraic solution of equations graphically; use intersection points of graphs to solve equations. <br> Understand and use proportional relationships and their graphs. | Graph to include simple cubic and quartic functions, <br> e.g. sketch the graph with equation $y=x^{2}(2 x-1)^{2}$ <br> Students should be able to sketch the graphs of $y=\|a x+b\|$ <br> They should be able to use their graph. <br> For example, sketch the graph with equation $y=\|2 x-1\|$ and use the graph to solve the equation $\|2 x-1\|=x$ or the inequality $\|2 x-1\|>x$ <br> The asymptotes will be parallel to the axes e.g. the asymptotes of the curve with equation $y=\frac{2}{x+a}+b$ are the lines with equations $y=b$ and $x=-a$ <br> Direct proportion between two variables. <br> Express relationship between two variables using proportion " $\propto$ " symbol or using equation involving constant <br> e.g. the circumference of a semicircle is directly proportional to its diameter so $C \propto d$ or $C=k d$ and the graph of $C$ against $d$ is a straight line through the origin with gradient $\boldsymbol{k}$. |


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| 2 <br> Algebra and functions <br> continued | 2.8 | Understand and use composite functions; inverse functions and their graphs. | The concept of a function as a one-one or many-one mapping from $\mathbb{R}$ (or a subset of $\mathbb{R}$ ) to $\mathbb{R}$. The notation $\mathrm{f}: x \mapsto$ and $\mathrm{f}(x)$ will be used. Domain and range of functions. <br> Students should know that fg will mean 'do $g$ first, then $f^{\prime}$ and that if $\mathrm{f}^{-1}$ exists, then $\mathrm{f}^{-1} \mathrm{f}(x)=\mathrm{ff}^{-1}(x)=x$ <br> They should also know that the graph of $y=\mathrm{f}^{-1}(x)$ is the image of the graph of $y=\mathrm{f}(x)$ after reflection in the line $y=x$ |
|  | 2.9 | Understand the effect of simple transformations on the graph of $y=\mathrm{f}(x)$, including sketching associated graphs: $\begin{aligned} & y=a f(x), \quad y=f(x)+a \\ & y=f(x+a), y=f(a x) \end{aligned}$ <br> and combinations of these transformations | Students should be able to find the graphs of $y=\|\mathrm{f}(x)\|$ and $y=\|\mathrm{f}(-x)\|$, given the graph of $y=\mathrm{f}(x)$. <br> Students should be able to apply a combination of these transformations to any of the functions in the A Level specification (quadratics, cubics, quartics, reciprocal, $\frac{a}{x^{2}},\|x\|, \sin x, \cos x, \tan x, \mathrm{e}^{x}$ and $a^{x}$ ) and sketch the resulting graph. <br> Given the graph of $y=\mathrm{f}(x)$, students should be able to sketch the graph of, e.g. $y=2 \mathrm{f}(3 x)$, or $y=\mathrm{f}(-x)+1$, <br> and should be able to sketch (for example) $y=3+\sin 2 x, y=-\cos \left(x+\frac{\pi}{4}\right)$ |
|  | 2.10 | Decompose rational functions into partial fractions (denominators not more complicated than squared linear terms and with no more than 3 terms, numerators constant or linear). | Partial fractions to include denominators such as <br> $(a x+b)(c x+d)(e x+f)$ and $(a x+b)(c x+d)^{2}$ <br> Applications to integration, differentiation and series expansions. |


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| $\mathbf{2}$ | 2.11 | Use of functions in modelling, <br> including consideration of <br> Algebra and <br> functions <br> continued | For example, use of trigonometric <br> functions for modelling tides, hours of <br> the models. |
| sunlight, etc. Use of exponential functions |  |  |  |
| for growth and decay (see Paper 1, |  |  |  |
| Section 6.7). Use of reciprocal function for |  |  |  |
| inverse proportion (e.g. pressure and |  |  |  |
| volume). |  |  |  |

