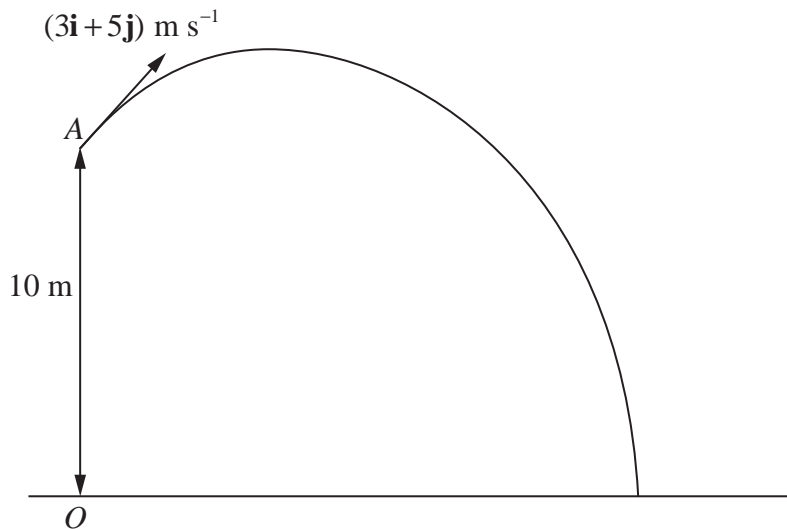


6. [In this question, the unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are in a vertical plane,  $\mathbf{i}$  being horizontal and  $\mathbf{j}$  being vertically upwards.]



**Figure 3**

At time  $t = 0$ , a particle  $P$  is projected from the point  $A$  which has position vector  $10\mathbf{j}$  metres with respect to a fixed origin  $O$  at ground level. The ground is horizontal. The velocity of projection of  $P$  is  $(3\mathbf{i} + 5\mathbf{j}) \text{ m s}^{-1}$ , as shown in Figure 3. The particle moves freely under gravity and reaches the ground after  $T$  seconds.

- (a) For  $0 \leq t \leq T$ , show that, with respect to  $O$ , the position vector,  $\mathbf{r}$  metres, of  $P$  at time  $t$  seconds is given by

$$\mathbf{r} = 3t\mathbf{i} + (10 + 5t - 4.9t^2)\mathbf{j} \quad (3)$$

- (b) Find the value of  $T$ . (3)

- (c) Find the velocity of  $P$  at time  $t$  seconds ( $0 \leq t \leq T$ ). (2)

When  $P$  is at the point  $B$ , the direction of motion of  $P$  is  $45^\circ$  below the horizontal.

- (d) Find the time taken for  $P$  to move from  $A$  to  $B$ . (2)

- (e) Find the speed of  $P$  as it passes through  $B$ . (2)

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[illegible]



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Diagram illustrating the path of a particle from point  $O$  to point  $A$ . The path is a semi-circular arc starting at  $O$  and ending at a point on the horizontal line. Point  $B$  is the projection of  $A$  onto the horizontal line. The initial velocity vector is  $(6\mathbf{i} + 12\mathbf{j}) \text{ m s}^{-1}$ .

The point  $O$  is a fixed point on a horizontal plane. A ball is projected from  $O$  with velocity  $(6\mathbf{i} + 12\mathbf{j}) \text{ m s}^{-1}$ , and passes through the point  $A$  at time  $t$  seconds after projection. The point  $B$  is on the horizontal plane vertically below  $A$ , as shown in Figure 3. It is given that  $OB = 2AB$ .

(a) the value of  $t$ ,

(7)

(b) the speed,  $V \text{ m s}^{-1}$ , of the ball at the instant when it passes through A.

(5)

At another point  $C$  on the path the speed of the ball is also  $V \text{ m s}^{-1}$ .

(c) Find the time taken for the ball to travel from  $O$  to  $C$ .

(3)

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### Question 7 continued



The diagram shows a quarter-circle arch with its center at point  $O$ . The vertical height from the ground to  $O$  is  $52.5\text{ m}$ . The horizontal distance from the ground to the base of the arch is  $50\text{ m}$ . A dashed horizontal line from  $O$  to the arch is  $10\text{ m}$  below the peak. A vector arrow points from  $O$  to the peak of the arch.

A small stone is projected from a point  $O$  at the top of a vertical cliff  $OA$ . The point  $O$  is 52.5 m above the sea. The stone rises to a maximum height of 10 m above the level of  $O$  before hitting the sea at the point  $B$ , where  $AB = 50$  m, as shown in Figure 4. The stone is modelled as a particle moving freely under gravity.

- (a) Show that the vertical component of the velocity of projection of the stone is  $14 \text{ m s}^{-1}$ . (3)
- (b) Find the speed of projection. (9)
- (c) Find the time after projection when the stone is moving parallel to  $OB$ . (5)







6.

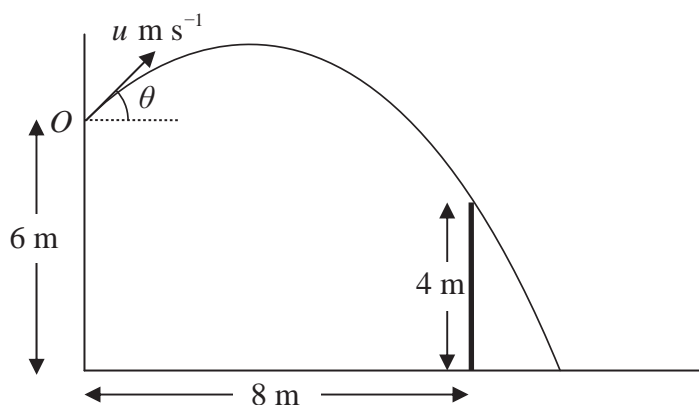


Figure 2

A ball is thrown from a point  $O$ , which is 6 m above horizontal ground. The ball is projected with speed  $u \text{ m s}^{-1}$  at an angle  $\theta$  above the horizontal. There is a thin vertical post which is 4 m high and 8 m horizontally away from the vertical through  $O$ , as shown in Figure 2. The ball passes just above the top of the post 2 s after projection. The ball is modelled as a particle.

(a) Show that  $\tan \theta = 2.2$  (5)

(b) Find the value of  $u$ . (2)

The ball hits the ground  $T$  seconds after projection.

(c) Find the value of  $T$ . (3)

Immediately before the ball hits the ground the direction of motion of the ball makes an angle  $\alpha$  with the horizontal.

(d) Find  $\alpha$ . (5)

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6.

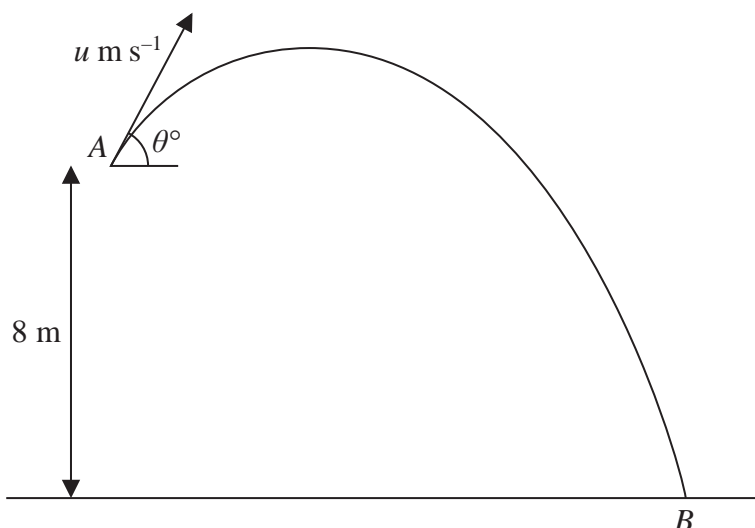


Figure 4

A ball is projected from a point  $A$  which is  $8\text{ m}$  above horizontal ground as shown in Figure 4. The ball is projected with speed  $u\text{ m s}^{-1}$  at an angle  $\theta^\circ$  above the horizontal. The ball moves freely under gravity and hits the ground at the point  $B$ . The speed of the ball immediately before it hits the ground is  $2u\text{ m s}^{-1}$ .

- (a) By considering energy, find the value of  $u$ . (5)

The time taken for the ball to move from  $A$  to  $B$  is  $2$  seconds. Find

- (b) the value of  $\theta$ , (4)

- (c) the minimum speed of the ball on its path from  $A$  to  $B$ . (2)

The first part of this question is outside the new syllabus and requires the relationship: gain in kinetic energy = loss in gravitational potential energy

$$0.5mv^2 - 0.5mu^2 = mgh$$



