

Expanding Brackets

Consider $2(3+4)$

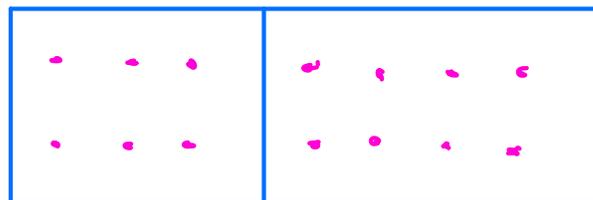
This means 2 multiplied by the value of the bracket

$$\text{So } 2 \times 7 = 14$$

We can think of this as 2 rows of 7 dots

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But we can also think of it as



$$\begin{aligned} \therefore 2(3+4) \\ &= 2 \times 3 + 2 \times 4 \\ &= 6 + 8 = 14 \end{aligned}$$

Algebra Examples

$$1) \quad 2(x+y) = 2x + 2y$$

$$2) \quad 3(x+4) = 3x + 12$$

Common wrong answers

$$3(x+4) = 3x + 7$$

$$3(x+4) = 3x + 4$$

Multiplication of Signed Numbers

+ve positive

$$+ve \times +ve \rightarrow +ve$$

-ve negative

$$-ve \times -ve \rightarrow +ve$$

$$+ve \times -ve \rightarrow -ve$$

$$-ve \times +ve \rightarrow -ve$$

Examples

$$1) \quad 4(y+2) = 4y + 8$$

$$2) \quad 5(2x+3) = 10x + 15$$

$$3) \quad 3(x-4) = 3x - 12$$

$$4) \quad 2(3x+y) = 6x + 2y$$

$$5) \quad 5(2p-1) = 10p - 5$$

$$6) \quad 6(x-3) = 6x - 18$$

$$7) \quad 3(2p-q) = 6p - 3q$$

$$8) \quad 5(x+y+2) = 5x + 5y + 10$$

$$9) \quad -3(2m-n) = -6m + 3n$$

$$10) \quad -2(x-y+4) = -2x + 2y - 8$$

Exercise A

Expand the brackets

- 1) $2(m+4) = 2m+8$
- 2) $3(h+2) = 3h+6$
- 3) $4(p+q) = 4p+4q$
- 4) $5(x+2) = 5x+10$
- 5) $3(2y+1) = 6y+3$
- 6) $2(p+4q) = 2p+8q$
- 7) $4(h+2k) = 4h+8k$
- 8) $6(2x+3) = 12x+18$
- 9) $3(x+2y+3) = 3x+6y+9$
- 10) $2(p+q+r) = 2p+2q+2r$

Expand the brackets

- 1) $4(x-1) = 4x-4$
- 2) $2(2x-3) = 4x-6$
- 3) $3(x-3) = 3x-9$
- 4) $5(2p-q) = 10p-5q$
- 5) $2(p-q+r) = 2p-2q+2r$
- 6) $-2(x+4) = -2x-8$
- 7) $-3(y-2) = -3y+6$
- 8) $-5(x-1) = -5x+5$
- 9) $-4(2x+y) = -8x-4y$
- 10) $-2(3p-2q) = -6p+4q$

Expand and Simplify

$$\begin{aligned} \text{Ex1} \quad & 2(x+3) + 3(x+5) \\ & = 2x+6 + 3x+15 \\ & = 5x+21 \end{aligned}$$

$$\begin{aligned} \text{Ex2} \quad & 5(p+2q) + 2(p+q) \\ & = 5p+10q + 2p+2q \\ & = 7p+12q \end{aligned}$$

$$\begin{aligned} \text{Ex3} \quad & 2(y-3) + 4(y+2) \\ & = 2y-6 + 4y+8 \\ & = 6y+2 \end{aligned}$$

$$\begin{aligned} \text{Ex4} \quad & 3(x+5) - 2(x+1) \\ & = 3x+15 - 2x-2 \\ & = x+13 \end{aligned}$$

$$\begin{aligned} \text{Ex5} \quad & 5(2x+y) - 2(x-y) \\ & = 10x+5y - 2x+2y \\ & = 8x+7y \end{aligned}$$

$$\begin{aligned} \text{Ex6} \quad & 3(p+2q) - (p+q) \\ & = 3p+6q - p-q \\ & = 2p+5q \end{aligned}$$

Exercise C

Expand and simplify

$$1) \quad 3(x+2) + 5(x+3)$$

$$2) \quad 4(p+2q) + 3(p+q)$$

$$3) \quad 3(x+2y) + 2(2x-y)$$

$$4) \quad 2(h+k) - 3(h-k)$$

$$5) \quad 5(x+6) - 2(x+4)$$

$$6) \quad -4(x-2y) + 3(x-1)$$

$$7) \quad 2(p+q+5) - 3(p+4)$$

$$8) \quad 5(h+2k) + 2(h+3k)$$

$$9) \quad 2(p+2q+3r) - 3(p-r)$$

$$10) \quad -4(x+2y) + 3(y+6)$$

$$\begin{aligned} 1) \quad & 3(x+2) + 5(x+3) \\ & = 3x + 6 + 5x + 15 \\ & = 8x + 21 \end{aligned}$$

$$\begin{aligned} 2) \quad & 4(p+2q) + 3(p+q) \\ & = 4p + 8q + 3p + 3q \\ & = 7p + 11q \end{aligned}$$

$$\begin{aligned} 3) \quad & 3(x+2y) + 2(2x-y) \\ & = 3x + 6y + 4x - 2y \\ & = 7x + 4y \end{aligned}$$

$$\begin{aligned} 4) \quad & 2(h+k) - 3(h-k) \\ & = 2h + 2k - 3h + 3k \\ & = -h + 5k \end{aligned}$$

$$\begin{aligned} 5) \quad & 5(x+6) - 2(x+4) \\ & = 5x + 30 - 2x - 8 \\ & = 3x + 22 \end{aligned}$$

$$\begin{aligned} 6) \quad & -4(x-2y) + 3(x-1) \\ & = -4x + 8y + 3x - 3 \\ & = -x + 8y - 3 \end{aligned}$$

$$\begin{aligned} 7) \quad & 2(p+q+s) - 3(p+4) \\ & = 2p + 2q + 10 - 3p - 12 \\ & = -p + 2q - 2 \end{aligned}$$

$$\begin{aligned} 8) \quad & 5(h+2k) + 2(h+3k) \\ & = 5h + 10k + 2h + 6k \\ & = 7h + 16k \end{aligned}$$

$$\begin{aligned} 9) \quad & 2(p+2q+3r) - 3(p-r) \\ & = 2p + 4q + 6r - 3p + 3r \\ & = -p + 4q + 9r \end{aligned}$$

$$\begin{aligned} 10) \quad & -4(x+2y) + 3(y+6) \\ & = -4x - 8y + 3y + 18 \\ & = -4x - 5y + 18 \end{aligned}$$