

Similar Figures

Ex A and B are similar figures

A has volume 439 cm^3 , B has volume 750 cm^3

- i) A length in A is 15 cm , find corresponding length in B
- ii) An area on B is 95 cm^2 , find corresponding area on A.

	A		B
Vol	439	:	750
	1	:	$\frac{750}{439}$
Length	1	:	$\sqrt[3]{\frac{750}{439}}$ 1.1955
Area	1	:	1.1955^2 1.4291

i) Length in B = $15 \times 1.1955 = 17.93 \text{ cm}$

ii) Area in A = $95 \div 1.4291 = 66.48 \text{ cm}^2$

Exercise C and D similar

Surface Areas C = 394 cm^2 D = 116 cm^2

A length on C = 23 cm , find corresponding length on D

A volume on D = 500 cm^3 , find corresponding volume on C

$$\begin{array}{r} \text{Area} \quad 394 : 116 \\ \hline 394 : 1 \end{array}$$

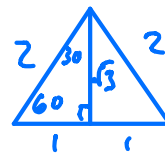
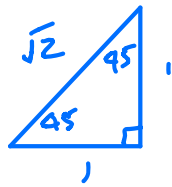
Length $\sqrt{\frac{394}{116}} \approx 1.84297$

Vol $1.84297^3 : 1$
 $6.25976 : 1$

Length $C = 23 \text{ cm}$ $D = 23 \div 1.84297$
 $= 12.48 \text{ cm}$

$$\text{Vol } D = 500 \text{ cm}^3 \quad C = 500 \times 6.25976 = 3130 \text{ cm}^3$$

	\sin	\cos	\tan
0°	0	1	0
30°	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$
45°	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	1
60°	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{1}$
90°	1	0	∞



$$\sin 30^\circ = \frac{x}{8}$$

$$8 \sin 30^\circ = x$$

$$8 \times \frac{1}{2} = x$$

$$x = 4 \text{ cm}$$

Compound Interest

John invests £630 for 5 years after which he has £883.61.

What was the annual rate of interest?

$$630 \times M^5 = 883.61$$

$$M^5 = \frac{883.61}{630}$$

$$M = \sqrt[5]{\frac{883.61}{630}} = \left(\frac{883.61}{630} \right)^{\frac{1}{5}}$$

$$= 1.07$$

Interest 7% per annum

Exercise

If £500 doubles in 8 years

What was the annual rate of increase to the nearest 0.1 of a per cent

$$500 \times M^8 = 1000$$

$$M^8 = \frac{1000}{500} = 2$$

$$M = 2^{\frac{1}{8}} = 1.090507733$$

$$\text{Rate of annual increase} = 9.1\%$$

Exercise

$$\begin{aligned} & (2x+1)(x-3)(x+2) \\ = & (2x^2+x-6x-3)(x+2) \\ = & (2x^2-5x-3)(x+2) \\ = & \begin{array}{l} 2x^3 - 5x^2 - 3x \\ + 4x^2 - 10x - 6 \end{array} \\ = & 2x^3 - x^2 - 13x - 6 \end{aligned}$$
