# AS Pure Mathematics 8MA0: Specimen Paper 1 Mark Scheme

Question	Scheme	Marks	AOs
1 (a)	$y = 2x^3 - 2x^2 - 2x + 8 \Rightarrow \frac{dy}{dx} = 6x^2 - 4x - 2$	M1	1.1b
	$\int_{-\infty}^{\infty} \frac{y - 2x}{2x} = \frac{2x + 6}{3x} = \frac{6x}{4x} = \frac{4x}{2x} = \frac{2x}{2x}$	A1	1.1b
		(2)	
(b)	Attempts $6x^2 - 4x - 2 > 0 \Rightarrow (6x + 2)(x - 1) > 0$	M1	1.1b
	$x = -\frac{1}{3}, 1$	A1	1.1b
	Chooses outside region	M1	1.1b
	$\left\{x:x<-\frac{1}{3}\right\}\cup\left\{x:x>1\right\}$	A1	2.5
		(4)	

(6 marks)

#### **Notes:**

(a)

M1: Attempts to differentiate. Allow for two correct terms un-simplified

**A1:**  $\frac{dy}{dx} = 6x^2 - 4x - 2$ 

**(b)** 

**M1:** Attempts to find the critical values of their  $\frac{dy}{dx} > 0$  or their  $\frac{dy}{dx} = 0$ 

**A1:** Correct critical values  $x = -\frac{1}{3}$ , 1

M1: Chooses the outside region

**A1:**  $\left\{ x : x < -\frac{1}{3} \right\} \cup \left\{ x : x > 1 \right\} \text{ or } \left\{ x : x \in \mathbb{R} \ x < -\frac{1}{3} \text{ or } x > 1 \right\}$ Accept also  $\left\{ x : x, -\frac{1}{3} \right\} \cup \left\{ x : x ... 1 \right\}$ 

Question	Scheme	Marks	AOs
2 (a)	$AB = OB - OA = 6\mathbf{i} - 3\mathbf{j} - (4\mathbf{i} + 2\mathbf{j})$	M1	1.1b
	$=2\mathbf{i}-5\mathbf{j}$	A1	1.1b
		(2)	
1(b)	Explains that $\overrightarrow{OC}$ is parallel to $\overrightarrow{AB}$ as $8\mathbf{i} - 20\mathbf{j} = 4 \times (2\mathbf{i} - 5\mathbf{j})$	M1	1.1b
	As $\overrightarrow{OC} = 4 \times AB$ it is parallel to it and not the same length Hence $OABC$ is a trapezium.	A1	2.4
		(2)	

(4 marks)

# **Notes:**

(a)

M1: Attempts AB = OB - OA or equivalent. This may be implied by one correct component

A1: 2i - 5j

**(b)** 

M1: Attempts to compare vectors  $\overrightarrow{OC}$  and  $\overrightarrow{AB}$  by considering their directions

**A1:** Fully explains why OABC is a trapezium. (The candidate is required to state that OC is parallel to AB but not the same length as it.)

Question	Scheme	Marks	AOs
3(a)	Uses or implies that $V = at + b$	B1	3.3
	Uses both $4 = 24a + b$ and $2.8 = 60a + b$ to get either a or b	M1	3.1b
	Uses both $4 = 24a + b$ and $2.8 = 60a + b$ to get both $a$ and $b$	M1	1.1b
	$\Rightarrow V = -\frac{1}{30}t + 4.8$	A1	1.1b
		(4)	
(b)	(i) States that the initial volume is 4.8 m <sup>3</sup>	B1 ft	3.4
	(ii) Attempts to solve $0 = -\frac{1}{30}t + 4.8$	M1	3.4
	States 144 minutes	A1	1.1b
		(3)	
(c)	<ul> <li>States any logical reason</li> <li>The tank will leak more quickly at the start due to the greater water pressure</li> <li>The hole will probably get larger and so will start to leak more quickly</li> <li>Sediment could cause the leak to be plugged and so the tank would not empty.</li> </ul>	B1	3.5b
		(1)	

## **Notes:**

(a)

**B1:** Uses or implies that V = at + b

You may award this at their final line but it must be V = f(t)

M1: Awarded for translating the problem in context and starting to solve. It is scored when both 4 = 24a + b and 2.8 = 60a + b are written down and the candidate proceeds to find either a or b. You may just see a line  $\pm \frac{4 - 2.8}{60 - 24}$ 

**M1:** Uses 4 = 24a + b and 2.8 = 60a + b to find both *a* and *b* 

**A1:**  $V = -\frac{1}{30}t + 4.8$  or exact equivalent. Eg 30V + t = 144

(b)(i)

**B1ft:** Follow through on their 'b'

(b)(ii)

**M1:** States that V = 0 and finds t by attempting to solve their  $0 = -\frac{1}{30}t + 4.8$ 

A1: States 144 minutes

(c)

B1: States any logical reason. There must be a statement and a reason that matches See scheme

Question	Scheme	Marks	AOs
4(a)	(4,-3)	B1	1.2
		(1)	
(b)	x = 6	B1	1.1b
		(1)	
(c)	x <b>4</b>	B1	1.1b
		(1)	
(d)	k > 1.5	B1	2.2a
		(1)	
		(4 n	narks)
Notes:			
See m/schei	ne		

Question	Scheme	Marks	AOs
5(a)	$f(-3) = (-3)^3 + 3 \times (-3)^2 - 4 \times (-3) - 12$	M1	1.1b
	$f(-3) = 0 \Rightarrow (x+3)$ is a factor $\Rightarrow$ Hence $f(x)$ is divisible by $(x+3)$ .	A1	2.4
		(2)	
(b)	$x^3 + 3x^2 - 4x - 12 = (x+3)(x^2 - 4)$	M1	1.1b
	=(x+3)(x+2)(x-2)	dM1 A1	1.1b 1.1b
		(3)	
(c)	$\frac{x^3 + 3x^2 - 4x - 12}{x^3 + 5x^2 + 6x} = \frac{\dots}{x(x^2 + 5x + 6)}$	M1	3.1a
	$=\frac{(x+3)(x+2)(x-2)}{x(x+3)(x+2)}$	dM1	1.1b
	$=\frac{(x-2)}{x}=1-\frac{2}{x}$	A1	2.1
		(3)	

#### **Notes:**

(a)

M1: Attempts f(-3)

A1: Achieves f(-3) = 0 and explains that (x+3) is a factor and hence f(x) is divisible by (x+3).

(b)

**M1:** Attempts to divide by (x+3) to get the quadratic factor.

By division look for the first two terms. ie  $x^2 + 0x$   $\frac{x^2 \pm 0x}{x+3)x^3 + 3x^2 - 4x - 12}$  $x^3 + 3x^2$ 

By inspection look for the first and last term  $x^3 + 3x^2 - 4x - 12 = (x+3)(x^2 + ...x \pm 4)$ 

**dM1:** For an attempt at factorising their  $(x^2-4)$ . (Need to check first and last terms)

**A1:** 
$$f(x) = (x+3)(x+2)(x-2)$$

(c)

M1: Takes a common factor of x out of the denominator and writes the numerator in factors.

Alternatively rewrites to 
$$x^3 + 3x^2 - 4x - 12 = A(x^3 + 5x^2 + 6x) + B(x^2 + 5x + 6)$$

dM1: Further factorises the denominator and cancels

Alternatively compares terms or otherwise to find either A or B

A1: Shows that  $\frac{x^3 + 3x^2 - 4x - 12}{x^3 + 5x^2 + 6x} = 1 - \frac{2}{x}$  with no errors or omissions

In the alternative there must be a reference to

$$x^{3} + 3x^{2} - 4x - 12 = 1\left(x^{3} + 5x^{2} + 6x\right) - 2\left(x^{2} + 5x + 6\right) \text{ and hence } \frac{x^{3} + 3x^{2} - 4x - 12}{x^{3} + 5x^{2} + 6x} = 1 - \frac{2}{x}$$

Question	Scheme	Marks	AOs
6(i)	Tries at least one value in the interval $Eg 4^{2}-4-1=11$	M1	1.1b
	States that when $n = 8$ it is FALSE and provides evidence $8^2 - 8 - 1 = 55 = (11 \times 5)$ Hence NOT PRIME	A1	2.4
		(2)	
(ii)	Knows that an odd number is of the form $2n+1$	B1	3.1a
	Attempts to simplify $(2n+1)^3 - (2n+1)^2$	M1	2.1
	and factorise $8n^3 + 8n^2 + 2n = 2(4n^3 + 4n^2 + 1n) =$	dM1	1.1b
	with statement 2× is always even	A1	2.4
		(4)	
Alt (ii)	Let the odd number be 'n' and attempts $n^3 - n^2$	B1	3.1a
	Attempts to factorise $n^3 - n^2 = n^2 (n-1)$	M1	2.1
	States that $n^2$ is odd (odd × odd) and $(n-1)$ is even (odd -1)	dM1	1.1b
	States that the product is even (odd×even)	A1	2.4

(6 marks)

## **Notes: See above**

(i)

M1: Attempts any  $n^2 - n - 1$  for *n* in the interval. It is acceptable just to show  $8^2 - 8 - 1 = 55$ A1: States that when n = 8 it is FALSE and provides evidence. A comment that  $55 = 11 \times 5$  and

hence not prime is required

(ii)

# See scheme for two examples of proof

Note that Alt (i) works equally well with an odd number of the form 2n-1

For example 
$$(2n-1)^3 - (2n-1)^2 = (2n-1)^2 \{2n-1-1\} = (2n-1)^2 \{2n-2\} = 2 \times (2n-1)^2 \{n-1\}$$

Question	Scheme	Marks	AOs
7 (a)	$\left(1 + \frac{3}{x}\right)^2 = 1 + \frac{6}{x} + \frac{9}{x^2}$	M1	1.1b
	$\begin{pmatrix} x \end{pmatrix} \qquad x \qquad x^2$	A1	1.1b
		(2)	
(b)	$\left[ \left( 1 + \frac{3}{4}x \right)^6 = 1 + 6 \times \left( \frac{3}{4}x \right) + \dots \right]$	B1	1.1b
	$\left  \left( 1 + \frac{3}{4}x \right)^6 = 1 + 6 \times \left( \frac{3}{4}x \right) + \frac{6 \times 5}{2} \times \left( \frac{3}{4}x \right)^2 + \frac{6 \times 5 \times 4}{3 \times 2} \times \left( \frac{3}{4}x \right)^3 + \dots \right $	M1	1.1b
		A1	1.1b
	$=1+\frac{9}{2}x+\frac{135}{16}x^2+\frac{135}{16}x^3+\dots$	A1	1.1b
		(4)	
(c)	$\left(1 + \frac{3}{x}\right)^2 \left(1 + \frac{3}{4}x\right)^6 = \left(1 + \frac{6}{x} + \frac{9}{x^2}\right) \left(1 + \frac{9}{2}x + \frac{135}{16}x^2 + \frac{135}{16}x^3 + \dots\right)$		
	Coefficient of $x = \frac{9}{2} + 6 \times \frac{135}{16} + 9 \times \frac{135}{16} = \frac{2097}{16}$	M1	2.1
	$\frac{2}{16} + \frac{1}{16} + \frac{1}{16} = \frac{1}{16}$	A1	1.1b
		(2)	

### **Notes:**

(a)

M1: Attempts 
$$\left(1 + \frac{3}{x}\right)^2 = A + \frac{B}{x} + \frac{C}{x^2}$$

**A1:** 
$$\left(1+\frac{3}{x}\right)^2 = 1+\frac{6}{x}+\frac{9}{x^2}$$

(h)

**B1:** First two terms correct, may be un-simplified

**M1:** Attempts the binomial expansion. Implied by the correct coefficient and power of x seen at least once in term 3 or 4

A1: Binomial expansion correct and un-simplified

A1: Binomial expansion correct and simplified.

(c)

**M1:** Combines all relevant terms for their  $\left(1 + \frac{A}{x} + \frac{B}{x^2}\right) \left(1 + Cx + Dx^2 + Ex^3 + ...\right)$  to find the

coefficient of x.

A1: Fully correct

Question	Scheme	Marks	AOs
8(a)	(i) $\int_{1}^{a} \sqrt{8x}  dx = \sqrt{8} \times \int_{1}^{a} \sqrt{x}  dx = 10\sqrt{8} = 20\sqrt{2}$	M1 A1	2.2a 1.1b
	(ii) $\int_{0}^{a} \sqrt{x}  dx = \int_{0}^{1} \sqrt{x}  dx + \int_{1}^{a} \sqrt{x}  dx = \left[ \frac{2}{3} x^{\frac{3}{2}} \right]_{0}^{1} + 10 = \frac{32}{3}$	M1 A1	2.1 1.1b
		(4)	
(b)	$R = \int_1^a \sqrt{x}  \mathrm{d}x = \left[\frac{2}{3}x^{\frac{3}{2}}\right]_1^a$	M1 A1	1.1b 1.1b
	$\frac{2}{3}a^{\frac{3}{2}} - \frac{2}{3} = 10 \Rightarrow a^{\frac{3}{2}} = 16 \Rightarrow a = 16^{\frac{2}{3}}$	dM1	3.1a
	$\Rightarrow a = 2^{4 \times \frac{2}{3}} = 2^{\frac{8}{3}}$	A1	2.1
		(4)	

#### **Notes:**

(a)(i)

M1: For deducing that  $\int_{1}^{a} \sqrt{8x} \, dx = \sqrt{8} \times \int_{1}^{a} \sqrt{x} \, dx$  attempting to multiply  $\int_{1}^{a} \sqrt{x} \, dx$  by  $\sqrt{8}$ 

**A1:**  $20\sqrt{2}$  or exact equivalent

(a)(ii)

**M1:** For identifying and attempting to use  $\int_0^a \sqrt{x} \, dx = \int_0^1 \sqrt{x} \, dx + \int_1^a \sqrt{x} \, dx$ 

**A1:** For  $\frac{32}{3}$  or exact equivalent

 $\overline{\text{(h)}}$ 

**M1:** Attempts to integrate,  $x^{\frac{1}{2}} \rightarrow x^{\frac{3}{2}}$ 

**dM1:** For a whole strategy to find a. In the scheme it is awarded for setting  $\left[ ...x^{\frac{3}{2}} \right]_{1}^{a} = 10$ , using both limits and proceeding using correct index work to find a. Alternatively a candidate could assume  $a = 2^{k}$ . In such a case it is awarded for setting  $\left[ ...x^{\frac{3}{2}} \right]_{1}^{2^{k}} = 10$ , using both limits and proceeding using correct index work to k = ...

**A1:**  $a = 2^{4 \times \frac{2}{3}} = 2^{\frac{8}{3}}$ 

In the alternative case, a further statement must be seen following  $k = \frac{8}{3}$  Hence True

Question	Scheme	Marks	AOs
9	$2\log_4(2-x) - \log_4(x+5) = 1$		
	Uses the power law $\log_4 (2-x)^2 - \log_4 (x+5) = 1$	M1	1.1b
	Uses the subtraction law $\log_4 \frac{(2-x)^2}{(x+5)} = 1$	M1	1.1b
	$\frac{(2-x)^2}{(x+5)} = 4 \rightarrow 3\text{TQ in } x$		3.1a
	$x^2 - 8x - 16 = 0$	A1	1.1b
	$\left(x-4\right)^2 = 32 \Longrightarrow x =$	M1	1.1b
	$x = 4 - 4\sqrt{2} \text{ oe only}$	A1	2.3
		(6)	

(6 marks)

#### **Notes:**

**M1:** Uses the power law of logs  $2\log_4(2-x) = \log_4(2-x)^2$ 

**M1:** Uses the subtraction law of logs following the above  $\log_4(2-x)^2 - \log_4(x+5) = \log_4\frac{(2-x)^2}{(x+5)}$ 

Alternatively uses the addition law following use of  $1 = \log_4 4$  That is  $1 + \log_4 (x+5) = \log_4 4(x+5)$ 

**dM1:** This can be awarded for the overall strategy leading to a 3TQ in x. It is dependent upon the correct use of both previous M's and for undoing the logs to reach a 3TQ equation in x

A1: For a correct equation in x

M1: For the correct method of solving their 3TQ = 0

**A1:**  $x = 4 - 4\sqrt{2}$  or exact equivalent only. (For example accept  $x = 4 - \sqrt{32}$ )

Question	Scheme	Marks	AOs
10(a)	Attempts to find the radius $\sqrt{(2-2)^2+(5-3)^2}$ or radius <sup>2</sup>	M1	1.1b
	Attempts $(x-2)^2 + (y-5)^2 = {r'}^2$	M1	1.1b
	Correct equation $(x-2)^2 + (y-5)^2 = 20$	A1	1.1b
		(3)	
(b)	Gradient of radius <i>OP</i> where <i>O</i> is the centre of $C = \frac{5-3}{22} = \left(\frac{1}{2}\right)$	M1	1.1b
	Equation of <i>l</i> is $-2 = \frac{y-3}{x+2}$	dM1	3.1a
	Any correct form $y = -2x - 1$	A1	1.1b
	Method of finding k Substitute $x = 2$ into their $y = -2x - 1$	M1	2.1
	k = -5	A1	1.1b
		(5)	

#### **Notes:**

(a)

M1: As scheme or states form of circle is  $(x-2)^2 + (y-5)^2 = {}^tr^2$ 

**M1:** As scheme or substitutes (-2,3) into  $(x-2)^2 + (y-5)^2 = {r'}^2$ 

A1: For a correct equation

If students use  $x^2 + y^2 + 2fx + 2gy + c = 0$  M1: f = 2, g = 5 M1: substitutes (2,5) to find value of c

A1: 
$$x^2 + y^2 - 4x - 10y + 9 = 0$$

(b)

M1: Attempts to find the gradient of OP where O is the centre of C

**dM1:** For a complete strategy of finding the equation of l using the perpendicular gradient to OP and the point (-2,3)..

**A1:** Any correct form of l Eg y = -2x - 1

M1: Scored for the key step of finding k. In this method they are required to substitute (2,k) in their y = -2x - 1 and solve for k.

**A1:** k = -5

Alt using Pythagoras' theorem

M1: Attempts Pythagoras to find both PQ and QQ in terms of k (where Q is centre of Q)

**dM1:** For the complete strategy of using Pythagoras theorem on triangle POQ to form an equation in k

**A1:** A correct equation in k Eg.  $20 + (k-3)^2 + 16 = (k-5)^2$ 

M1: Scored for a correct attempt to solve their quadratic to find k.

**A1:** k = -5

Question	Scheme	Marks	AOs
11(i)	$(2\theta + 10^{\circ}) = \arcsin(-0.6)$	M1	1.1b
	$(2\theta + 10^{\circ}) = -143.13^{\circ}, -36.87^{\circ}, 216.87^{\circ}, 323.13^{\circ} (Any two)$	A1	1.1b
	Correct order to find $\theta = \dots$		1.1b
	Two of $\theta = -76.6^{\circ}, -23.4^{\circ}, 103.4^{\circ}, 156.6^{\circ}$ .	A1	1.1b
	$\theta = -76.6^{\circ}, -23.4^{\circ}, 103.4^{\circ}, 156.6^{\circ}, \text{ only}$	A1	2.1
		(5)	
(ii)	(a) Explains that the student has not considered the negative value of $x = -29.0^{\circ}$ when solving $\cos x = \frac{7}{8}$	B1	2.3
	Explains that the student should check if any solutions of $\sin x = 0$ (the cancelled term) are solutions of the given equation. $x = 0^{\circ}$ should have been included as a solution	B1	2.3
	(b) Attempts to solve $4\alpha + 199^{\circ} = (360 - 29.0)^{\circ}$	M1	2.2a
	α = 33.0°	A1	1.1b
		(4)	

(9 marks)

## **Notes:**

(i)

M1: Attempts  $\arcsin(-0.6)$  implied by any correct answer

**A1:** Any two of -143.13°, -36.87°, 216.87°, 323.13°

**dM1:** Correct method to find any value of  $\theta$ 

**A1:** Any two of  $\theta = -76.6^{\circ}, -23.4^{\circ}, 103.4^{\circ}, 156.6^{\circ}$ .

**A1:** A full solution leading to all four answers and no extras  $\theta = -76.6^{\circ}, -23.4^{\circ}, 103.4^{\circ}, 156.6^{\circ}, \text{ only}$ 

(ii)(a)

**B1:** See scheme

**B1:** See scheme

(ii)(b)

M1: For deducing the smallest positive solution occurs when  $4\alpha + 199^{\circ} = (360 - 29.0)^{\circ}$ 

**A1:**  $\alpha = 33^{\circ}$ 

Question	Sch	eme	Marks	AOs
12(a)	$Sets 3x - 2\sqrt{x} = 8x - 16$		B1	1.1a
	$2\sqrt{x} = 16 - 5x$ $4x = (16 - 5x)^2 \Rightarrow x =$	$5x + 2\sqrt{x} - 16 = 0$ $\Rightarrow (5\sqrt{x} \pm 8)(\sqrt{x} \pm 2) = 0$	M1	3.1a
	$25x^2 - 164x + 256 = 0$	$\left(5\sqrt{x}-8\right)\left(\sqrt{x}+2\right)=0$	A1	1.1b
	$(25x-64)(x-4)=0 \Rightarrow x=$	$\sqrt{x} = \frac{8}{5}, (-2) \Rightarrow x = \dots$	M1	1.1b
	$x = \frac{64}{25} \text{ only}$		A1	2.3
			(5)	
(b)	Attempts to solve $3x - 2\sqrt{x} = 0$		M1	2.1
	Correct solution $x = \frac{4}{9}$ $y$ , $3x - 2\sqrt{x}$ , $y > 8x - 16$ $x = \frac{4}{9}$		A1	1.1b
			B1ft	1.1b
			(3)	

#### **Notes:**

(a)

B1: Sets the equations equal to each other and achieves a correct equation

M1: Awarded for the key step in solving the problem. This can be awarded via two routes. Both routes must lead to a value for x.

- Making the  $\sqrt{x}$  term the subject and squaring both sides (not each term)
- Recognising that this is a quadratic in  $\sqrt{x}$  and attempting to factorise  $\Rightarrow (5\sqrt{x} \pm 8)(\sqrt{x} \pm 2) = 0$

**A1:** A correct intermediate line  $25x^2 - 164x + 256 = 0$  or  $(5\sqrt{x} - 8)(\sqrt{x} + 2) = 0$ 

M1: A correct method to find at least one value for x. Way One it is for factorising (usual rules), Way Two it is squaring at least one result of their  $\sqrt{x}$ 

A1: Realises that  $x = \frac{64}{25}$  is the only solution  $x = \frac{64}{25}$ , 4 is A0

(b) **M1:** Attempts to solve  $3x - 2\sqrt{x} = 0$  For example

Allow 
$$3x = 2\sqrt{x} \Rightarrow 9x^2 = 4x \Rightarrow x = ...$$

Allow 
$$3x = 2\sqrt{x} \Rightarrow x^{\frac{1}{2}} = \frac{2}{3} \Rightarrow x = ...$$

**A1:** Correct solution to  $3x - 2\sqrt{x} = 0 \Rightarrow x = \frac{4}{9}$ 

**B1:** For a **consistent** solution defining R using either convention

Either 
$$y$$
,  $3x - 2\sqrt{x}$ ,  $y > 8x - 16$   $x = ... \frac{4}{9}$  Or  $y < 3x - 2\sqrt{x}$ ,  $y = ... 8x - 16$   $x > \frac{4}{9}$ 

Question	Scheme	Marks	AOs
13(a)	$0.2 \mathrm{m}^2$	B1	3.4
		(1)	
(b)	$A = 0.2e^{0.3t}$ Rate of change = gradient = $\frac{dA}{dt} = 0.06e^{0.3t}$	M1	3.1b
	At $t = 5 \Rightarrow$ Rate of Growth is $0.06e^{1.5} = 0.269 \text{ m}^2/\text{day}$	A1	1.1b
		(2)	
(c)	$100 = 0.2e^{0.3t} \Rightarrow e^{0.3t} = 500$	M1 A1	3.1a 1.1b
	$\Rightarrow t = \frac{\ln(500)}{0.3} = 20.7 \text{ days} \qquad 20 \text{ days } 17 \text{ hours}$	M1 A1	1.1b 3.2a
		(4)	0.20
	At $t = 5 \Rightarrow$ Rate of Growth is $0.06e^{1.5} = 0.269 \text{ m}^2/\text{day}$	A1	1.1b
		(2)	
(d)	The model given suggests that the pond is fully covered after 20 days 17 hours. Observed data is inconsistent with this as the pond is only 90% covered by the end of one month (28/29/30/31 days). Hence the model is not accurate	B1	3.5a
		(1)	

## **Notes:**

(a)

**B1:**  $0.2 \text{ m}^2$  oe

**(b)** 

**M1:** Links rate of change to gradient and differentiates  $0.2e^{0.3t} \rightarrow ke^{0.3t}$ 

A1: Correct answer 0.269 m<sup>2</sup>/day

(c)

**M1:** Substitutes A = 100 and proceeds to  $e^{0.3t} = k$ 

**A1:**  $e^{0.3t} = 500$ 

**M1:** Correct method when proceeding from  $e^{0.3t} = k \Rightarrow t = ...$ 

**A1:** 20 days 17 hours

(d)

**B1:** Valid conclusion following through on their answer to (c).

Question	Scheme	Marks	AOs
14	$y = (x-2)^2 (x+3) = (x^2 - 4x + 4)(x+3) = x^3 - 1x^2 - 8x + 12$	B1	1.1b
	An attempt to find $x$ coordinate of the maximum point. To score this you must see either  • an attempt to expand $(x-2)^2(x+3)$ , an attempt to differentiate the result, followed by an attempt at solving $\frac{dy}{dx} = 0$ • an attempt to differentiate $(x-2)^2(x+3)$ by the product rule followed by an attempt at solving $\frac{dy}{dx} = 0$	M1	3.1a
	$y = x^3 - 1x^2 - 8x + 12 \Rightarrow \frac{dy}{dx} = 3x^2 - 2x - 8$	M1	1.1b
	Maximum point occurs when $\frac{dy}{dx} = 0 \Rightarrow (x-2)(3x+4) = 0$	M1	1.1b
	$\Rightarrow x = -\frac{4}{3}$	A1	1.1b
	An attempt to find the area under $y = (x-2)^2 (x+3)$ between two values. To score this you must see an attempt to expand $(x-2)^2 (x+3)$ followed by an attempt at using two limits	M1	3.1a
	Area = $\int (x^3 - 1x^2 - 8x + 12) dx = \left[ \frac{x^4}{4} - \frac{x^3}{3} - 4x^2 + 12x \right]$	M1	1.1b
	Uses a top limit of 2 and a bottom limit of their $x = -\frac{4}{3} R = \left[ \frac{x^4}{4} - \frac{x^3}{3} - 4x^2 + 12x \right]_{-\frac{4}{3}}^2$	M1	2.2a
	$Uses = \frac{28}{3} - \frac{1744}{81} = \frac{2500}{81}$	A1	2.1
		(9)	

(9 marks)

# **Notes:**

**B1:** Expands  $(x-2)^2(x+3)$  to  $x^3-1x^2-8x+12$  seen at some point in their solution. It may appear just on their integral for example.

M1: This is a problem solving mark for knowing the method of finding the maximum point. You should expect to see the key points used (i) differentiation (ii) solution of their  $\frac{dy}{dx} = 0$ 

M1: For correctly differentiating their cubic with at least two terms correct (for their cubic).

M1: For setting their  $\frac{dy}{dx} = 0$  and solves using a correct method (including calculator methods)

**A1:** 
$$\Rightarrow x = -\frac{4}{3}$$

**M1:** This is a problem solving mark for knowing how integration is used to find the area underneath a curve between two points.

M1: For correctly integrating their cubic with at least two correct terms (for their cubic).

M1: For deducing the top limit is 2, the bottom limit is their  $x = -\frac{4}{3}$  and applying these correctly within their integration.

**A1:** Shows above steps clearly and proceeds to  $R = \frac{2500}{81}$