

Direct Proportion

There is direct proportion between two variables when one variable is a simple multiple of the other

$y \propto x$ means y is proportional to x

We write $y = kx$ for some constant k

Exercise 22A

Ex 1 T is directly proportional to M

$$T = 20 \text{ when } M = 4$$

Find the relationship between T and M

$$T = kM$$

$$\begin{aligned} T &= 20 \\ M &= 4 \end{aligned} \quad \left. \begin{aligned} 20 &= 4k \\ \frac{20}{4} &= k \\ 5 &= k \end{aligned} \right. \quad \therefore \quad \underline{T = 5M}$$

a) Find T when $M = 3$

$$T = 5 \times 3$$

$$\underline{T = 15}$$

b) Find M when $T = 10$

$$10 = 5M$$

$$\frac{10}{5} = M$$

$$\underline{M = 2}$$

Ex2 W is directly proportional to F

$$W=45 \text{ when } F=3$$

Find relationship between W and F

$$W = kF$$

$$\begin{cases} W=45 \\ F=3 \end{cases}$$

$$45 = 3k$$

$$\frac{45}{3} = k$$

$$15 = k$$

$$\underline{W = 15F}$$

a) Find W when F = 5

$$W = 15 \times 5$$

$$\underline{\underline{W = 75}}$$

b) Find F when W = 90

$$90 = 15F$$

$$\frac{90}{15} = F$$

$$\underline{F = 6}$$

3)

$$Q = kP$$

$$100 = 2k$$

$$\frac{100}{2} = k$$

$$50 = k$$

$$\begin{cases} Q = 100 \\ P = 2 \end{cases}$$

$$\underline{\underline{Q = 50P}}$$

a) Find Q when P = 3

$$Q = 50 \times 3$$

$$\underline{\underline{Q = 150}}$$

b) Find P when Q = 300

$$300 = 50P$$

$$\frac{300}{50} = P$$

$$\underline{P = 6}$$

$$5) D = \text{Distance} \quad T = \text{Time}$$

$$D = kT$$

$$105 = 3k$$

$$\frac{105}{3} = k$$

$$35 = k$$

$$\begin{cases} D = 105 \\ T = 3 \end{cases}$$

$$\underline{D = 35T}$$

$$\text{Find } D \text{ when } T = 5 \text{ hrs}$$

$$D = 35 \times 5$$

$$\underline{D = 175 \text{ miles}}$$

$$\text{Find } T \text{ when } D = 280 \text{ miles}$$

$$280 = 35T$$

$$\frac{280}{35} = T$$

$$\underline{T = 8 \text{ hrs}}$$

$$6) C = kW$$

$$\begin{cases} W = 250 \text{ kg} \\ C = £47.50 \end{cases}$$

$$47.5 = 250k$$

$$\frac{47.5}{250} = k$$

$$0.19 = k$$

$$C = 0.19W$$

$$\text{Find } C \text{ when } W = 350 \text{ kg}$$

$$C = 0.19 \times 350$$

$$C = £66.50$$

$$\text{Find } W \text{ when } C = £33.25$$

$$33.25 = 0.19W$$

$$\frac{33.25}{0.19} = W$$

$$\underline{W = 175 \text{ kg}}$$

D) T is directly proportional to x^2

$$T = 36 \text{ when } x = 3$$

Find relationship between T and x.

$$T = kx^2$$

$$\begin{aligned} T &= 36 \\ x &= 3 \end{aligned}$$

$$36 = k \times 3^2$$

$$36 = 9k$$

$$\frac{36}{9} = k$$

$$4 = k$$

$$\underline{\quad T = 4x^2 \quad}$$

a) Find T when $x=5$

$$T = 4 \times 5^2$$

$$T = 100$$

b) Find x when $T=400$

$$400 = 4x^2$$

$$\frac{400}{4} = x^2$$

$$100 = x^2$$

$$\sqrt{100} = x$$

$$x = \pm 10$$

3) E varies directly \sqrt{C}

$$E = 40 \text{ when } C = 25$$

Find relationship connecting E to C

$$E = k\sqrt{C}$$

$$\begin{cases} E = 40 \\ C = 25 \end{cases}$$

$$40 = K\sqrt{25}$$

$$40 = 5K$$

$$\frac{40}{5} = K$$

$$\underline{E = 8\sqrt{C}}$$

a) Find E when $C=49$

$$E = 8\sqrt{49}$$

$$E = 8 \times 7$$

$$E = 56$$

b) Find C when $E=10.4$

$$10.4 = 8\sqrt{C}$$

$$\frac{10.4}{8} = \sqrt{C}$$

$$1.3 = \sqrt{C}$$

$$1.3^2 = C$$

$$\underline{C = 1.69}$$