Probability scale


Roll a Die
Outcome 123456
Probability $\frac{1}{6} \quad \frac{1}{6} \quad \frac{1}{6} \quad \frac{1}{6} \quad \frac{1}{6} \quad \frac{1}{6}$
These 6 outcomes use mutually exclusive events
Consider $\operatorname{Prob}(2$ or 3$)=\frac{2}{6}=\frac{1}{6}+\frac{1}{6}$
'OR' Rule for mutually exclusive events

$$
\operatorname{Prob}(\text { even number })=\frac{1}{6}+\frac{1}{6}+\frac{1}{6}=\frac{3}{6}=\frac{1}{2}
$$

We cannot add together the probabilities of events which are not mutually exclusive

Let $A$ be event even number $(2,4,6)$
$B$ be event numb $>3(4,5,6)$

$$
\operatorname{Prob}(A \text { or } B) \neq P(A)+P(B)
$$

$$
\frac{3}{6}+\frac{3}{6}=1
$$

In fact $P(A$ or $B)$ wart ter $A$ a

$$
=\frac{4}{6}
$$

The reason $t$ lis does not work e is that $A$ and $\mathbb{A}$ are not mutually exclusive - they overlap $P(A \cap B)=\frac{2}{6}$ as they have $A, 6$ in common

Venn
Diagram


Monopoly Dice
Roll a blue die and a red die and add their scores $t_{0}$ find a tot

| Blue |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
|  | 1 | 2 | 3 | 4 | 5 | 6 |
|  | 2 | 3 | 4 | 5 | 6 | 7 |
|  | 3 | 4 | 5 | 6 | 2 | 8 |
| 3 | 4 | 5 | 6 | 2 | 8 | 9 |
| 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 6 | 7 | 8 | 9 | 10 | 11 | 12 |

$$
\begin{array}{ll}
P(2)=\frac{1}{36} & P(8)=\frac{5}{36} \\
P(3)=\frac{2}{36} & P(9)=\frac{4}{36} \\
P(4)=\frac{3}{36} & P(10)=\frac{3}{36} \\
P(5)=\frac{4}{36} & P(11)=\frac{2}{36} \\
P(6)=\frac{5}{36} & P(12)=\frac{1}{36} \\
P(7)=\frac{6}{36} & P(\text { Prime tatar } \\
\text { Find }=\frac{15}{36} \\
& P(7)=\frac{6}{36} \text { or } \frac{1}{6}
\end{array}
$$

Draw a sample space diagram for when two dice are rolled and the numbers are multiplied together

Blue

| $x$ | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\operatorname{led}$ | 1 | 2 | 3 | 4 | 5 | 6 |
|  | 2 | 4 | 6 | 8 | 10 | 12 |
|  | 3 | 6 | 9 | 12 | 15 | 18 |
| 4 | 4 | 8 | 12 | 16 | 20 | 24 |
| 5 | 5 | 10 | 15 | 20 | 25 | 30 |
| 6 | 6 | 12 | 18 | 24 | 30 | 36 |

Find $P$ (Even) $=\frac{27}{36}=\frac{3}{4}$

$$
P(\text { Divisib6 by } 6) \frac{15}{36}=\frac{5}{12}
$$

Draw a sample space to show rolling two dice and taking the lower score from the higher score. Score $O$ if both the same

| - | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 0 | 1 | 2 | 3 | 4 | 5 |
| 2 | 1 | 0 | 1 | 2 | 3 | 4 |
| 3 | 2 | 1 | 0 | 1 | 2 | 3 |
| 4 | 3 | 2 | 1 | 0 | 1 | 2 |
| 5 | 4 | 3 | 2 | 1 | 0 | 1 |
| 6 | 5 | 4 | 3 | 2 | 1 | 0 |

$$
\text { Find } \begin{aligned}
P\left(E_{\text {ven }}\right) & =\frac{18}{36} \\
P(\text { Prime }) & =\frac{16}{36}
\end{aligned}
$$

