

Questions

Q1.

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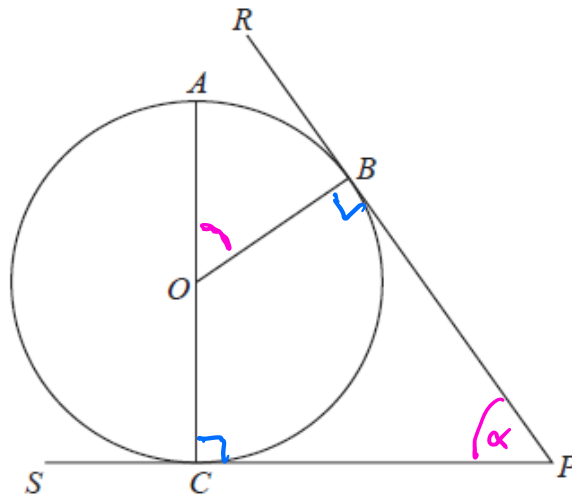


Diagram NOT
accurately drawn

$$\text{Let } \angle CPB = \alpha$$

$$\angle PCO = \angle PBO = 90^\circ$$

(tangent - radius)

A, B and C are points on a circle, centre O.

RBP is the tangent to the circle at B.
SCP is the tangent to the circle at C.
AOC is a diameter of the circle.

Prove that angle AOB is equal to angle CPB.
You must give reasons at each stage.

$$\begin{aligned} \therefore \angle COB &= 360 - 90 - 90 - \alpha \\ &= 180 - \alpha \\ &\text{ (} \angle \text{ sum of quad)} \end{aligned}$$

$$\angle AOB = 180 - \angle COB$$

(Total for question = 5 marks)

(Angles on straight line)

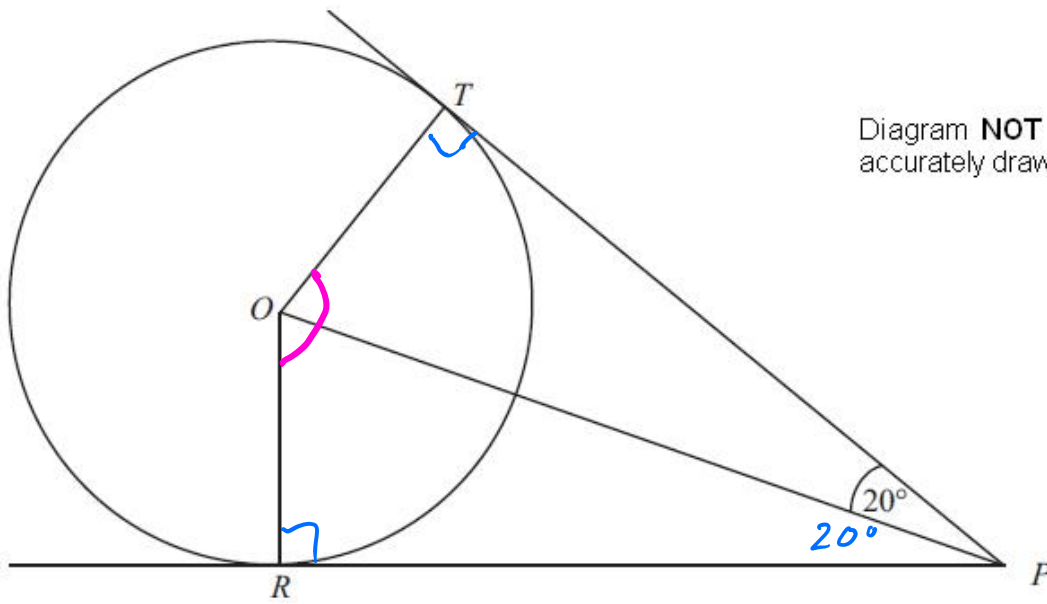
$$180 - (180 - \alpha) = \alpha$$

$$\therefore \angle AOB = \angle CPB$$

Q2.

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Diagram **NOT**
accurately drawn



T and R are two points on a circle centre O.

PT and PR are the tangents to the circle from P.

Angle TPO = 20° .

Work out the size of angle TOR.

You must give reasons for each stage of your working.

$$\angle PRO = \angle PTO = 90^\circ \text{ (tangent radius)}$$

$$\angle RPO = 20^\circ \text{ (symmetry or congruent } \Delta s)$$

$$\angle TOR = 360 - 90 - 90 - 40$$

(\angle sum of quad)

$$\underline{\underline{\angle TOR = 140^\circ}}$$

(Total for Question is 4 marks)

Q3.

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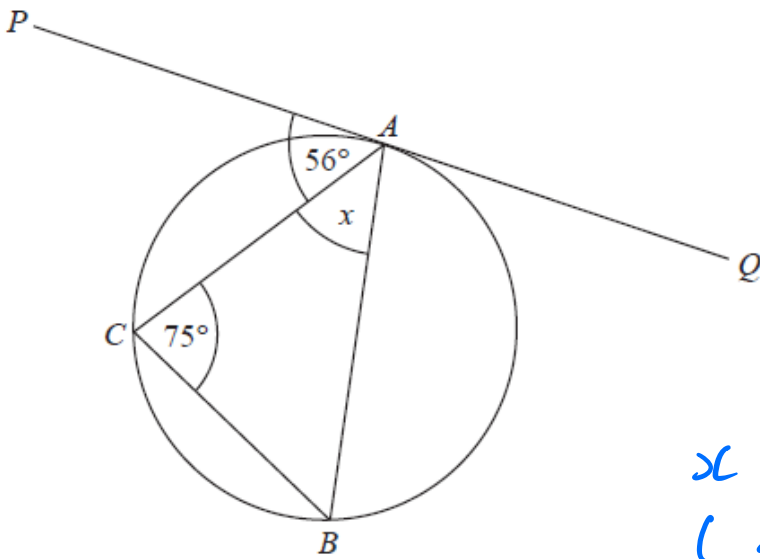


Diagram NOT
accurately drawn

$$\angle ABC = 56^\circ$$

(alt seg theorem)

$$x = 180^\circ - 75^\circ - 56^\circ$$

(\angle sum of Δ)

$$\underline{x = 49^\circ}$$

A, B and C are points on the circumference of a circle.
The straight line PAQ is a tangent to the circle.
Angle PAC = 56°
Angle ACB = 75°

Work out the size of the angle marked x.
Give reasons for each stage of your working.

(Total for question = 3 marks)

Q4.

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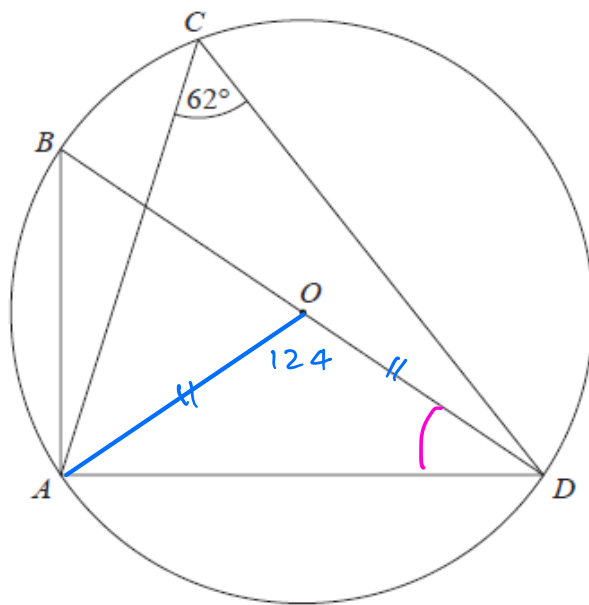


Diagram NOT
accurately drawn

$$\angle AOB = 124^\circ$$

(\angle at centre
twice \angle at circ)

$$\angle ADB = \frac{180 - 124}{2}$$

(base \angle s of isos Δ)

A, B, C and D are points on the circumference of a circle, centre O.
BOD is a straight line.
Angle ACD = 62°

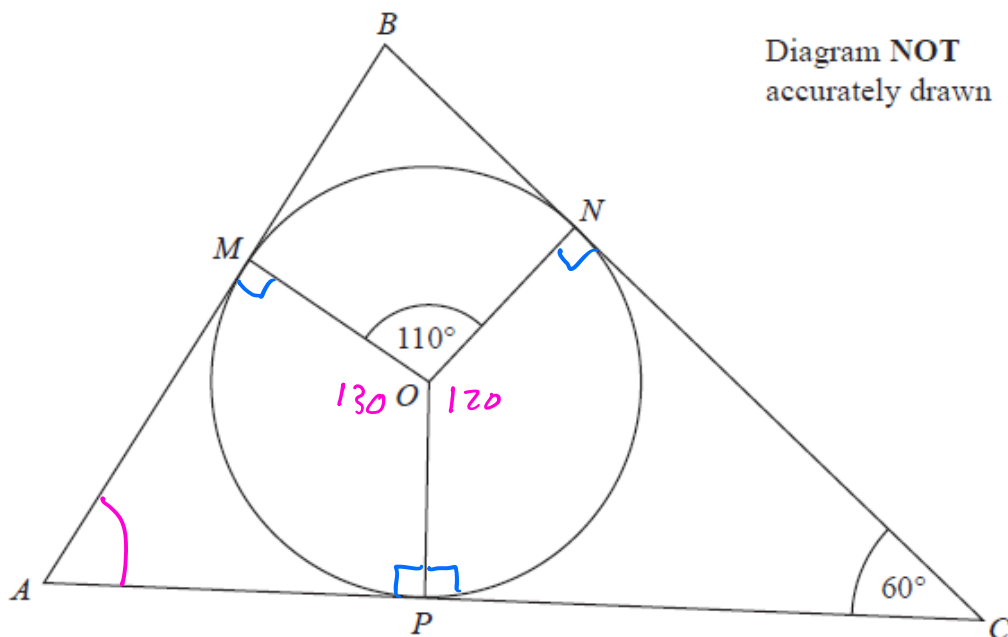
$$\underline{\angle ADB = 28^\circ}$$

Find the size of angle ADB .
Give a reason for each stage in your working.

(Total for question = 4 marks)

Q5.

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M , N and P are points on the circumference of a circle, centre O .
 AMB , BNC , and CPA are tangents to the circle.

Angle $MON = 110^\circ$
Angle $BCA = 60^\circ$

$$\angle CPO = \angle CNO = \angle APO = \angle AMO = 90^\circ$$

(tangent - radius)

Work out the size of angle BAC .
Give reasons for each stage of your working.

$$\angle PON = 360 - 90 - 90 - 60 = 120^\circ \quad (\angle \text{sum of quad})$$

(Total for question = 4 marks)

$$\angle MOP = 360 - 110 - 120 = 130^\circ \quad (\angle \text{s at a point})$$

$$\angle BAC = 360 - 90 - 90 - 130 = 50^\circ \quad (\angle \text{sum of quad})$$

$$\underline{\underline{\angle BAC = 50^\circ}}$$