

Introduction to Algebraic Proof

1) Prove $\text{odd} + \text{odd} = \text{even}$

Let $2n$ be an even integer
where n is an integer

$2n+1$ is an odd integer

$2m+1$ is an odd integer
where m integer

$\text{odd} + \text{odd}$

$$\begin{aligned} 2n+1 + 2m+1 &= 2n + 2m + 2 \\ &= 2(n+m+1) \end{aligned}$$

2 is a factor

\therefore even

2) $\text{even} + \text{odd} = \text{odd}$

$$\begin{aligned} 2n + 2m+1 &= 2n + 2m + 1 \\ &= 2(n+m) + 1 \end{aligned}$$

3 & 5

6 & 8

$n \quad n+1 \quad n+2$

Prove the sum of 3 consecutive integers
is divisible by 3

$$\begin{aligned}n + n + 1 + n + 2 &= 3n + 3 \\ &= 3(n+1)\end{aligned}$$

\therefore a multiple of 3
