Linear Equations

Ex 1

$$
\begin{aligned}
& x+2=6 \\
& x+2-2=6 \\
& x=6-2 \\
& x=4
\end{aligned}
$$

Ex

$$
\begin{aligned}
2 x & =10 \\
\frac{2 x}{2} & =\frac{10}{2} \\
x & =\frac{10}{2} \\
x & =5
\end{aligned}
$$

$E \times 4$

Ex

$$
\begin{aligned}
& 2 x+3=11 \quad E \times 6 \quad 5 x-3=17 \\
& 2 x=11-3 \\
& 2 x=8 \\
& x=\frac{8}{2} \\
& x=4 \\
& 5 x=17+3 \\
& 5 x=20 \\
& x=\frac{20}{5} \\
& x=4
\end{aligned}
$$

$$
\begin{aligned}
\frac{x}{4} & =8 \\
\frac{x}{4} \times 4 & =8 \times 4 \\
x & =8 \times 4 \\
x & =32
\end{aligned}
$$

1) $x+9=11$
2) $2 x+5=19$
3) $x-3=4$
4) $3 x-2=16$
5) $3 x=12$
6) $4 x+3=23$
7) $\frac{x}{2}=5$
8) $5 x-7=43$
9) $x+1=8$
10) $x-5=7$
11) $6 x+2=20$
12) $7 x=21$
13) $\frac{x}{3}=5$
14) $x+4=1$
15) $x-5=-4$
16) $2 x=15$
17) $\frac{x}{10}=4$
18) 

$$
\begin{aligned}
& x+9=11 \\
& x=11-9 \\
& x=2
\end{aligned}
$$

2) 

$$
\begin{aligned}
& x-3=4 \\
& x=4+3 \\
& x=7
\end{aligned}
$$

3) 

$$
\begin{aligned}
3 x & =12 \\
x & =\frac{12}{3} \\
x & =4
\end{aligned}
$$

4) 

$$
\begin{aligned}
& \frac{x}{2}=5 \\
& x=5 \times 2 \\
& x=10
\end{aligned}
$$

5) 

$$
\begin{aligned}
& x+1=8 \\
& x=8-1 \\
& x=7
\end{aligned}
$$

6) 

$$
\begin{aligned}
& x-5=7 \\
& x=7+5 \\
& x=12
\end{aligned}
$$

7) 

$$
\begin{aligned}
7 x & =21 \\
x & =\frac{21}{7} \\
x & =3
\end{aligned}
$$

8) 

$$
\begin{aligned}
& \frac{x}{3}=5 \\
& x=5 \times 3 \\
& x=15
\end{aligned}
$$

9) 

$$
\begin{aligned}
& x+4=1 \\
& x=1-4 \\
& x=-3
\end{aligned}
$$

10) 

$$
\begin{aligned}
& x-5=-4 \\
& x=-4+5 \\
& x=1
\end{aligned}
$$

11) 

$$
\begin{aligned}
2 x & =15 \\
x & =\frac{15}{2} \\
x & =7 \frac{1}{2}
\end{aligned}
$$

12) 

$$
\begin{aligned}
& \frac{x}{10}=4 \\
& x=4 \times 10 \\
& x=40
\end{aligned}
$$

13) 

$$
\begin{aligned}
& 2 x+5=19 \\
& 2 x=19-5 \\
& 2 x=14 \\
& x=\frac{14}{2} \\
& x=7
\end{aligned}
$$

$$
\text { 14) } 3 x-2=16
$$

$$
3 x=16+2
$$

$$
3 x=18
$$

$$
x=\frac{18}{3}
$$

$$
x=6
$$

$$
\text { 15) } 4 x+3=23
$$

$$
4 x=23-3
$$

$$
4 x=20
$$

$$
x=\frac{20}{4}
$$

$$
x=5
$$

16) $5 x-7=43$
$5 x=43+7$
$5 x=50$
$x=\frac{50}{5}$
$x=10$
17) $6 x+2=20$
$6 x=20-2$
$6 x=18$
$x=\frac{18}{6}$
$x=3$
18) $7 x-5=23$
$7 x=23+5$
$7 x=28$
$x=\frac{28}{7}$
$x=4$
linear equations I
ExERcISE
19) 

$$
\begin{aligned}
& 2 x-7=8 \\
& 2 x=8+7 \\
& 2 x=15 \\
& x=\frac{15}{2} \\
& x=7 \frac{1}{2}
\end{aligned}
$$

20) 

$$
\begin{aligned}
& 3 x+5=19 \\
& 3 x=19-5 \\
& 3 x=14 \\
& x=\frac{14}{3} \\
& x=4 \frac{2}{3}
\end{aligned}
$$

Equs with an $x$ term on both sides Ex 7

Ex 8

$$
\begin{aligned}
7 x+8 & =3 x+56 \\
7 x-3 x & =+56-8 \\
4 x & =48 \\
x & =\frac{48}{4} \\
x & =12
\end{aligned}
$$

$$
5 x+32=14-5 x
$$

$$
5 x+5 x=14-32
$$

$$
10 x=-18
$$

$$
x=-\frac{18}{10}
$$

$$
x=-1.8
$$

or $-1 \frac{8}{10}$
or $-1 \frac{4}{5}$

Equations Involving Brackets
$E \times 9$

$$
\begin{array}{ll}
3(2 x+1)=33 & \text { or } \\
6 x+3=33 & 3(2 x+1)=33 \\
6 x=33-3 & 2 x+1=\frac{33}{3} \\
6 x=30 & 2 x+1=11 \\
x=\frac{30}{6} & 2 x=11-1 \\
x=5 & 2 x=10 \\
& x=\frac{10}{2} \\
& x=5
\end{array}
$$

Ex 10

$$
\begin{aligned}
2(5 x+3) & =3(x+1)+17 \\
10 x+6 & =3 x+3+17 \\
10 x-3 x & =+3+17-6 \\
7 x & =14 \\
x & =\frac{14}{7} \\
x & =2
\end{aligned}
$$

linear equations (2)

Solve the following equations:

1. $3 x-7=23$
2. $5 x+3=25$
3. $8 x-2=4 x+10$
4. $3 x+7=27-x$
5. $\quad 9 x-3=7 x+8$
6. $2 x-5=16-5 x$
7. $\quad 2(x+3)=18$
8. $\quad 4(x-5)=8$
9. $3(2 x+7)=30$
10. $\quad 5(2 x-3)=25$

LINEAR EQUATIONS (2)
EXERCISE
1.

$$
\begin{aligned}
& 3 x-7=23 \\
& 3 x=23+7 \\
& 3 x=30 \\
& x=\frac{30}{3} \\
& x=10
\end{aligned}
$$

2. 

$$
\begin{aligned}
& 5 x+3=25 \\
& 5 x=25-3 \\
& 5 x=22 \\
& x=\frac{22}{5} \\
& x=4 \frac{2}{5}
\end{aligned}
$$

3. 

$$
\begin{aligned}
8 x-2 & =4 x+10 \\
8 x-4 x & =+10+2 \\
4 x & =12 \\
x & =\frac{12}{4} \\
x & =3
\end{aligned}
$$

Linear equations (z)
EXERCISE
7. $2(x+3)=18$
$2 x+6=18$
$2 x=18-6$
$2 x=12$
$x=\frac{12}{2}$
$x=6$
8. $\quad 4(x-5)=8$
$4 x-20=8$
$4 x=8+20$
$4 x=28$

$$
x=\frac{28}{4}
$$

$$
x=7
$$

9. 

$$
\begin{aligned}
& 3(2 x+7)=30 \\
& 6 x+21=30 \\
& 6 x=30-21 \\
& 6 x=9 \\
& x=\frac{9}{6} \\
& x=1 \frac{3}{6} \text { or } x=1 \frac{1}{2}
\end{aligned}
$$

10. 

$$
\begin{aligned}
& 5(2 x-3)=25 \\
& 10 x-15=25 \\
& 10 x=25+15 \\
& 10 x=40 \\
& x=\frac{40}{10} \\
& x=4
\end{aligned}
$$

Word Problems Involving Linear Equations

Ex Alan is twice as old as Bill
Colin is 5 years older than Alan
Colin is 17. How old is Bill?
Let Bill be $x$ years old

$$
\begin{aligned}
\text { Alan } & =2 x \\
\text { coli } & =2 x+5 \\
2 x+5 & =17 \\
2 x & =17-5 \\
2 x & =12 \\
x & =\frac{12}{2} \quad x=6
\end{aligned}
$$

Bill is 6 years old

Ex 2 John's dad is 3 times as old as John In 12 years time dad will be twice as old as John. How old is John now?

Let Join be $x$ now
Dad now $3 x$
In 12 years time John $x+12$

$$
3 x+12=2(x+12)
$$

$$
\begin{gathered}
3 x+12=2 x+24 \\
3 x-2 x=24-12 \\
x=12
\end{gathered}
$$

John is now 12 years old
13. The sum of three consecutive odd integers is 189 . What are the integers?

Let lowest be $x$
the others are $x+2, x+4$

$$
\begin{gathered}
x+x+2+x+4=189 \\
3 x+6=189 \\
3 x=189-6 \\
3 x=183 \\
x=\frac{183}{3} \\
x=61
\end{gathered}
$$

Numbers are $61,63,65$

