

Exercise 10.45 Q1

$$\begin{aligned}
 \text{a) } x^3 - x^2 &= 200 \\
 x^3 &= x^2 + 200 \\
 x &= \sqrt[3]{x^2 + 200} \\
 x_{n+1} &= \sqrt[3]{x_n^2 + 200}
 \end{aligned}$$

Try  $x = 10$

$$x_1 = \sqrt[3]{10^2 + 200} = 6.694$$

$$x_2 = \sqrt[3]{6.694^2 + 200} = 6.256$$

$$x_3 = \sqrt[3]{6.256^2 + 200} = 6.207$$

$$x_4 = \sqrt[3]{6.207^2 + 200} = 6.202$$

$x = 6.202$   
is approximate  
root

Exercise 10.45 Q2, 3, 4, 5

$$\begin{aligned}
 \text{2a) i) } p(p+1) &= 100 \\
 p^2 + p &= 100 \\
 p^2 &= 100 - p \\
 p &= \sqrt{100 - p} \\
 p_{n+1} &= \sqrt{100 - p_n}
 \end{aligned}$$

$$\begin{aligned}
 \text{ii) } p(p+1) &= 100 \\
 p^2 + p &= 100 \\
 p &= 100 - p^2
 \end{aligned}$$

Let  $p_0 = 9$

$$p_1 = \sqrt{100 - 9} = 9.539$$

$$p_2 = \sqrt{100 - 9.539} = 9.511$$

$$p_3 = \sqrt{100 - 9.511} = 9.513$$

$$p \approx 9.51$$

Let  $p_0 = 9$

$$p_{n+1} = 100 - p_n^2$$

$$p_1 = 100 - 9^2 = 19$$

$$p_2 = 100 - 19^2 = -261$$

$$p_3 = 100 - (-261)^2 = -68021$$

This  
formula  
does not  
lead to a  
root!