

Quadratic Sequences

Exercise 21.25

1 a) First term 2
Add consecutive
odd numbers

2, 3, 6, 11

1 b) First term 5
Add consecutive
even numbers

5, 7, 11, 17

2 a) Find next two terms

3, 7, 13, 21, 31, 43

2 b) 4, 6, 10, 16, 24, 34

3 a) Find missing term

6, 12, 22, 36, 54

3 b) 2 8, 18, 32, 50

4 a) i) Find first 3 terms and 10th term

$$T(n) = n^2 + 3$$

$$1^2 + 3$$

$$2^2 + 3$$

$$3^2 + 3$$

$$10^2 + 3$$

$$4$$

$$7$$

$$12$$

$$103$$

$$\text{ii) } T(n) = n^2 + 2n$$

$$1^2 + 2(1)$$

$$2^2 + 2(2)$$

$$3^2 + 2(3)$$

$$10^2 + 2(10)$$

$$3$$

$$8$$

$$15$$

$$120$$

$$\text{vii) } 2n^2 + 2n + 2$$

$$2(1)^2 + 2(1) + 2 = 2 + 2 + 2 = 6$$

$$2(2)^2 + 2(2) + 2 = 8 + 4 + 2 = 14$$

$$2(3)^2 + 2(3) + 2 = 18 + 6 + 2 = 26$$

$$2(4)^2 + 2(4) + 2 = 32 + 8 + 2 = 42$$

6g

$$6 \quad 14 \quad 26 \quad 42$$

$$2n^2 \quad 2 \quad 8 \quad 18 \quad 32$$

$$4 \quad 6 \quad 8 \quad 10$$

$$+2n \quad 2 \quad 4 \quad 6 \quad 8$$

$$+2 \quad 2 \quad 2 \quad 2 \quad 2$$

$$2n^2 + 2n + 2$$

7a)

$$\begin{array}{rcccc} & & -2 & & -2 \\ & & -3 & -5 & -7 \\ & 9, & 6, & 1, & -6 \\ -n^2 & -1 & -4 & -9 & -16 \\ \hline +10 & 10 & 10 & 10 & 10 \end{array}$$

$$n^{\text{th}} \text{ term} = -n^2 + 10$$

7c)

$$\begin{array}{rcccc} & & -2 & & -2 \\ & & -2 & -4 & -6 \\ & 0 & -2 & -6 & -12 \\ -n^2 & -1 & -4 & -9 & -16 \\ \hline +n & 1 & 2 & 3 & 4 \end{array}$$

$$n^{\text{th}} \text{ term} = -n^2 + n$$

9) Is 150 in sequence generated by $n^2 + 3$

$$\text{If } n^2 + 3 = 150$$

$$n^2 = 150 - 3$$

$$n^2 = 147$$

$$n = \sqrt{147}$$

$$n = 12.124 \quad \text{not a whole number}$$

So answer is no
